

# **Broadening of adiabatic droplet spectra through eddy hopping: Polluted versus pristine environments**

**Wojciech W. Grabowski,  
with Kamal Kant Chandrakar and Hugh Morrison**

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submitted to JAS



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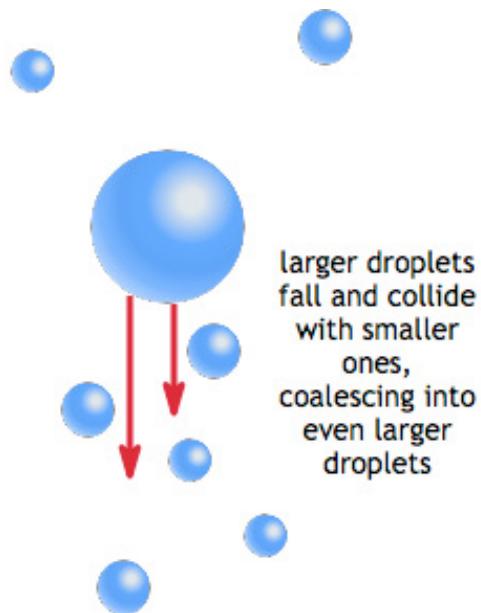
Width of the cloud droplet spectrum in warm clouds is an important parameter.

It affects transfer of solar radiation through a cloud and collision/coalescence that leads to rain formation...

Effective radius  $r_e$ :

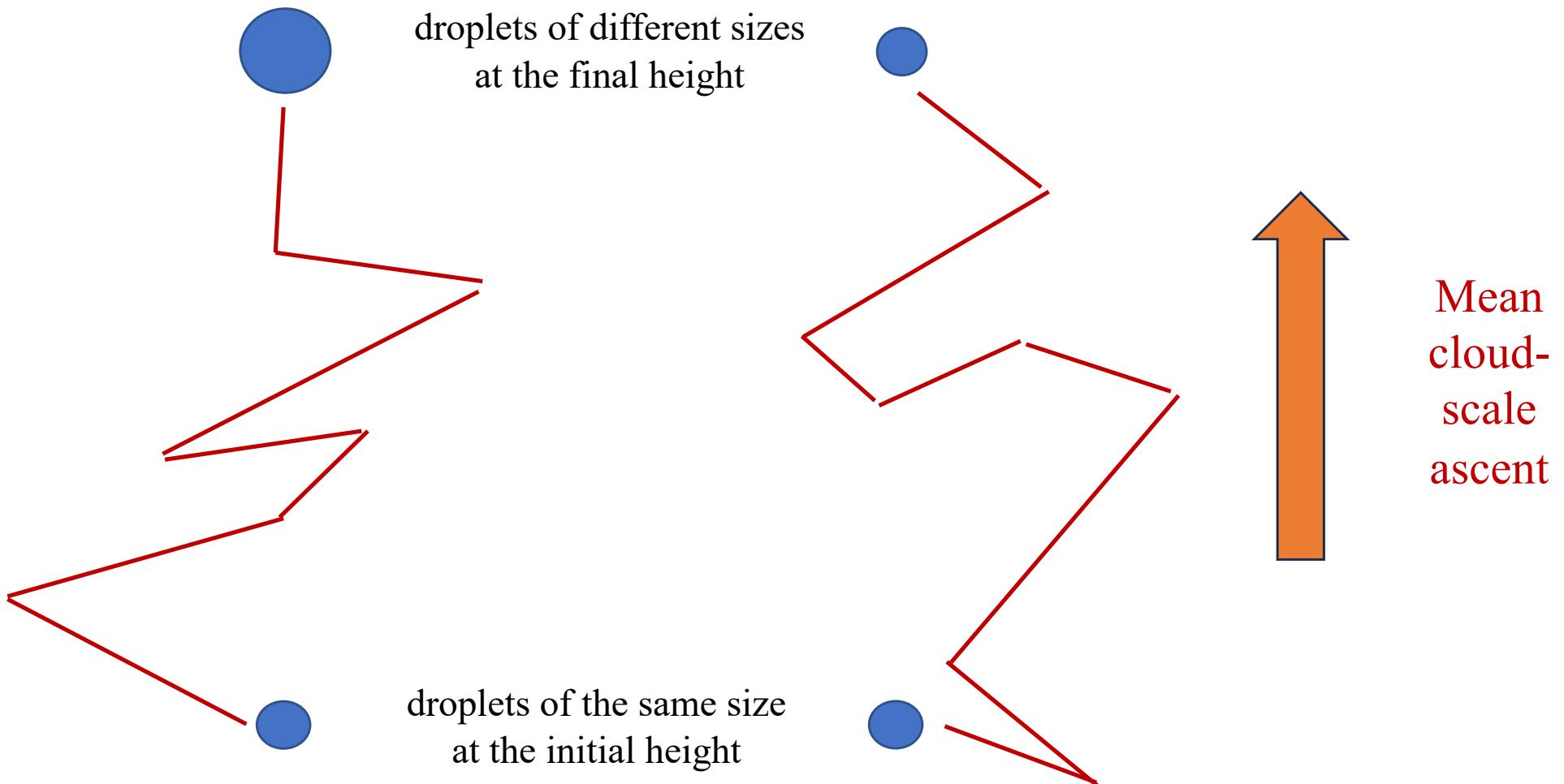
$$r_e = \frac{\int_0^\infty \pi r^3 \cdot n(r) dr}{\int_0^\infty \pi r^2 \cdot n(r) dr}$$

Gravitational droplet collisions:



# CLOUD DROPLETS HOPPING TURBULENT EDDIES

“Stochastic condensation”



## Observed and/or simulated adiabatic droplet spectra in different CCN environments:

Fitzgerald, PhD dis., 1972: comparison between observed and simulated droplet spectra (sic!)

Jensen et al. *J. Atmos. Sci.*, 1985: CCOPE project: observed (and simulated) droplet spectra

Miles et al. *J. Atmos. Sci.*, 2000: database of observed stratus cloud droplet size distributions

Brenguier and Chaumat, *J. Atmos. Sci.*, 2001, adiabatic broadening theory and observations

Yum and Hudson *Atmos. Res.* 2005: observed and simulated droplet spectra from several projects

Pawlowska et al. *Geophys. Res. Lett.*, 2006: observed droplet spectra from ACE2 field project

Prabha et al. *J. Geophys. Res.*, 2012: observed droplet spectra from CAIPEEX field project

Chandrakar et al. *Proc. Nat. Ac. Sci.* 2016: Pi chamber observations

Thomas et al. *JAMES*: 2019: Pi chamber observations and simulations

Grabowski *J. Atmos. Sci.*, 2020: Pi chamber simulations with monodisperse dry CCN

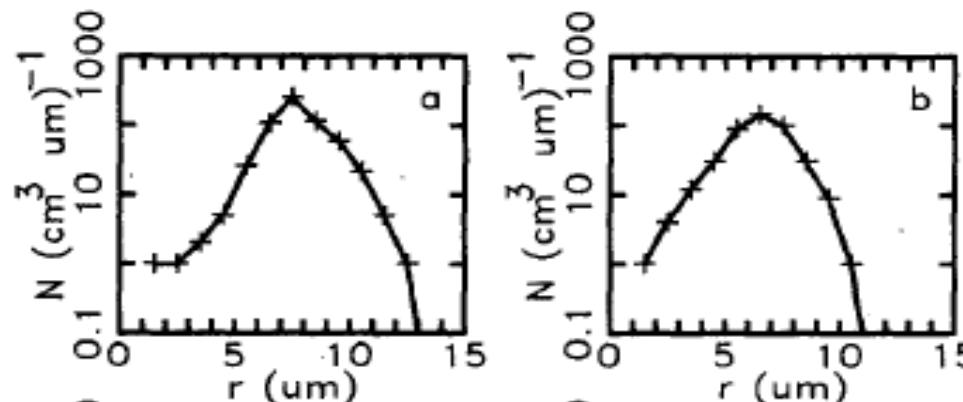
Grabowski et al. *J. Atmos. Sci.*, 2024: Pi chamber simulations with CCN distribution

Chandrakar et al. *J. Atmos. Sci.* 2020, 2021, 2022: cumulus congestus simulations

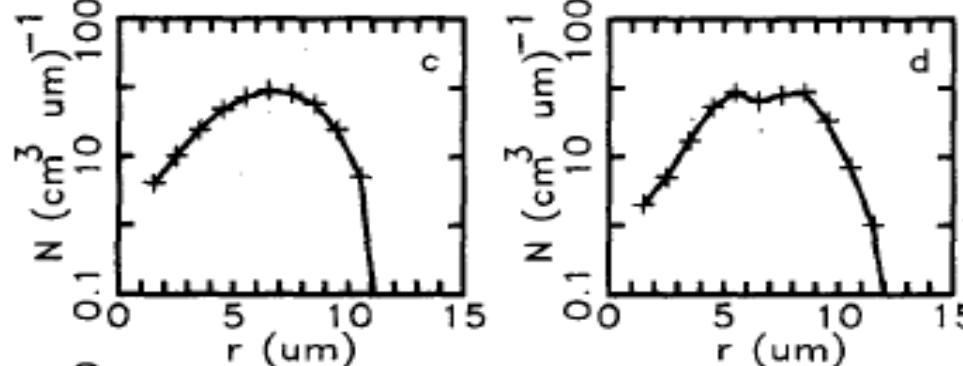
Grabowski et al. *J. Atmos. Sci.* 2025: 1D model of eddy hopping with superdroplets

Observed **close-to-adiabatic** cloud droplet spectra in a cumulus averaged over  $\sim 100$  m (1 Hz, FSSP data) around 1 km above the cloud base:

observed,  
adiabatic fraction  
 $AF \approx 1$ ;  $\sigma_r = 1.3 \mu\text{m}$

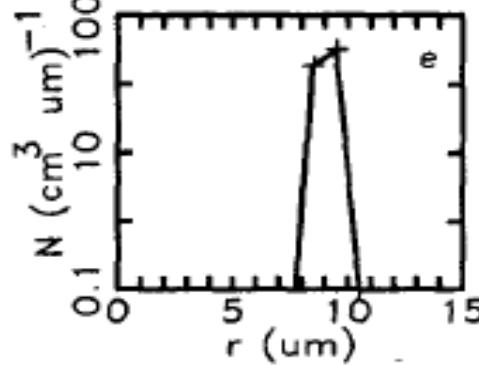


observed, AF  $\approx 0.8$ ;  
 $\sigma_r = 1.8 \mu\text{m}$



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 $\sigma_r = 1.3 \mu\text{m}$

observed, AF  $\approx 1$ ;  
bimodal

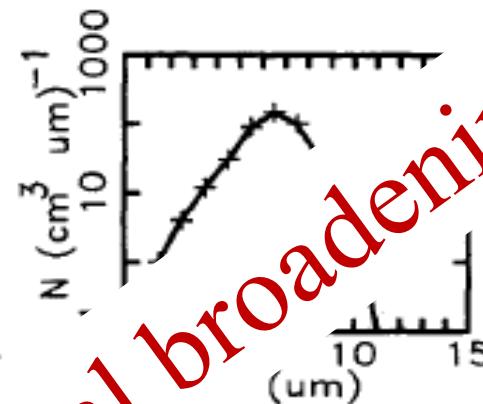
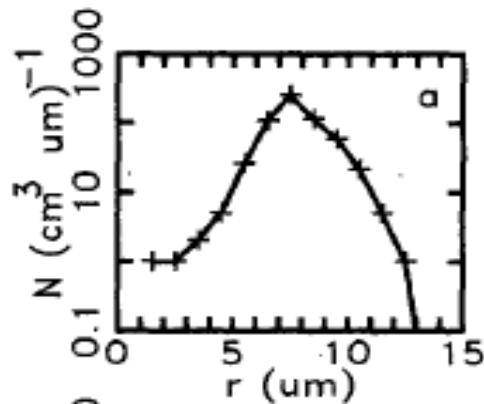


(Jensen et al. *JAS* 1985)

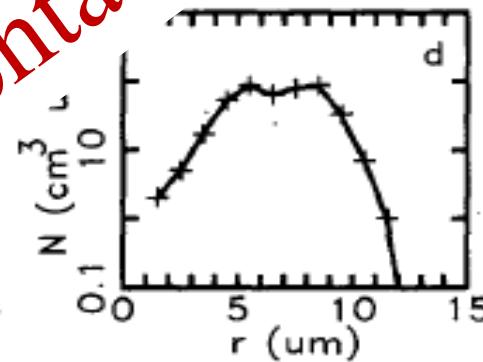
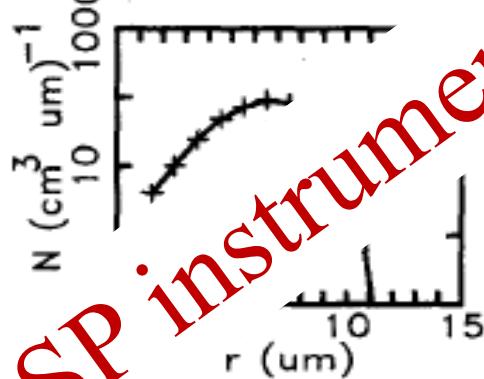


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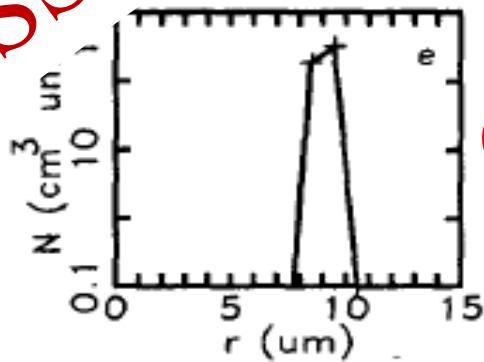


observed,  $AF \approx 0.8$ ;  
 $\sigma_r = 1.8 \mu\text{m}$



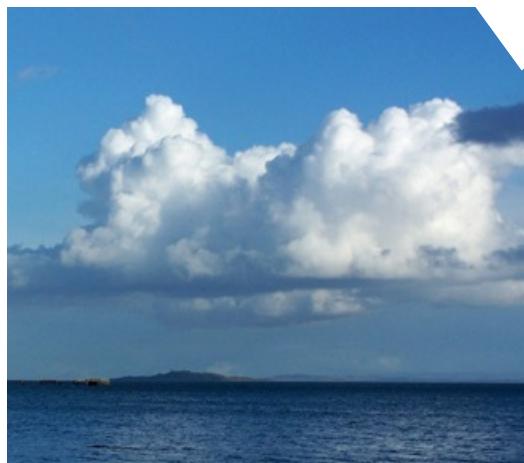
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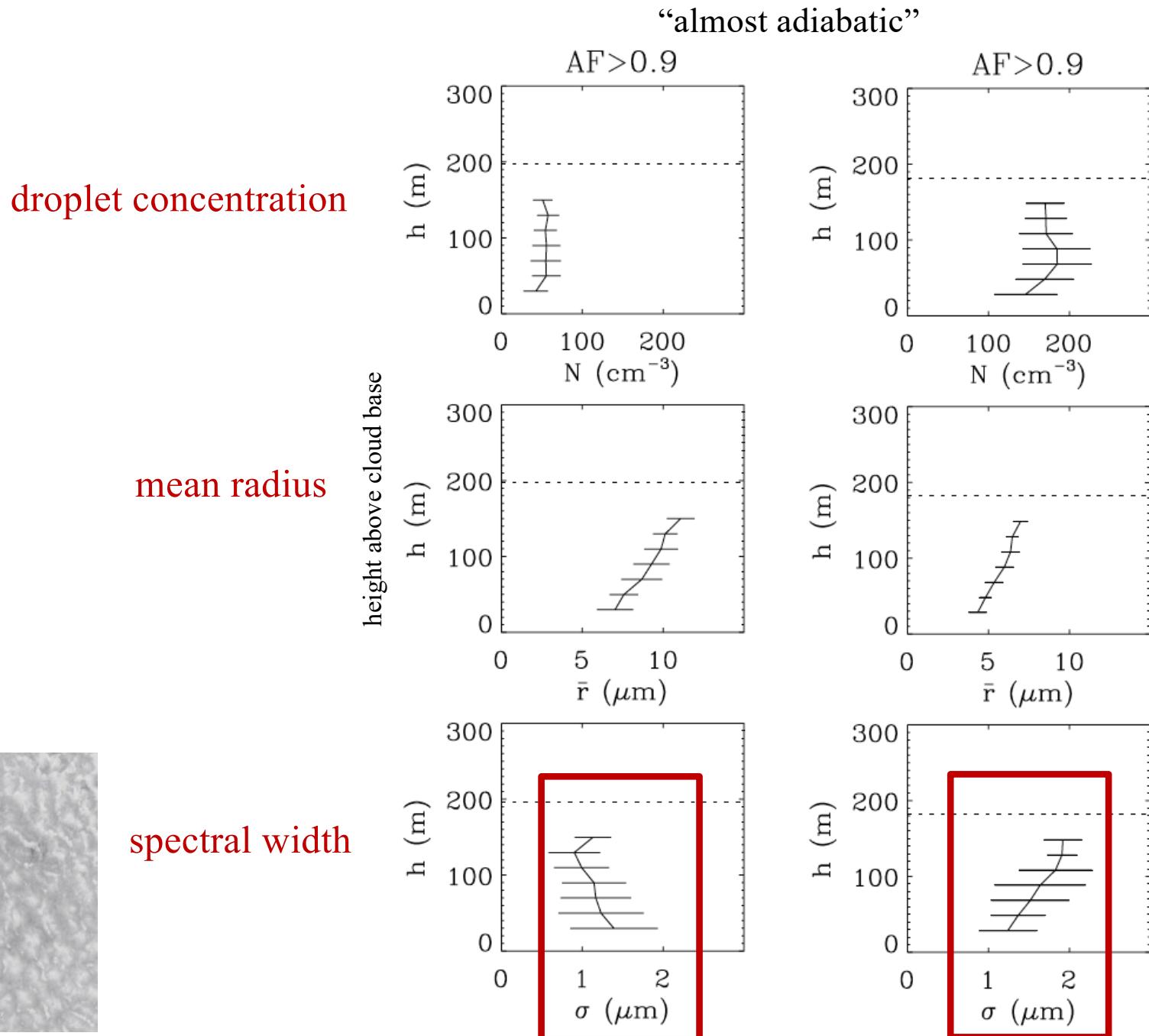
calculated adiabatic  
spectrum;  $\sigma_r = 0.1 \mu\text{m}$

FSSP instrumental broadening?



(Jensen et al. *JAS* 1985)

Observed close-to-adiabatic cloud droplet spectra in **stratocumulus** averaged over  $\sim 10$ m (10 Hz, **Fast FSSP**; Pawlowska et al. *GRL* 2006):



Field  
projects

Table 2

Same as Table 1 except the parameters are measured or estimated averages of all data for each of the eight different field projects or air masses

Project name	$N_{CCN}$ (cm $^{-3}$ )	$S_{eff}$ (%)	$N_c(ave)$ (cm $^{-3}$ )	MD ( $\mu m$ )	$\sigma_c$ ( $\mu m$ )	diameter
Sc	1411	0.100	312	10.9	4.6	
Xc	1061	0.040	183	8.0	3.7	
Sm	359	0.095	150	15.0	4.8	
A	202	0.150	58	13.6	4.3	
Xm	195	0.310	86	11.9	4.9	
S2	191	0.180	70	13.9	5.0	
F	122	0.080	41	15.0	4.8	
S1	32	0.920	28	17.1	6.7	

The  $S_{eff}$  is the effective supersaturation (Hudson, 1984) based on the average droplet concentration,  $N_c(ave)$ .

Adiabatic  
parcel  
simulations

Table 1

Average CCN concentrations at 1%  $S$  ( $N_{CCN}$ ) for the eight field projects or air masses used in this study and cloud microphysical parameter values [maximum supersaturation ( $S_{max}$ ), activated cloud droplet concentration ( $N_c$ ), cloud droplet mean diameter (MD) and standard deviation of cloud droplet diameter ( $\sigma_c$ )] obtained from the Robinson (1984) model runs after 150 m ascent with 50 cm s $^{-1}$  updraft

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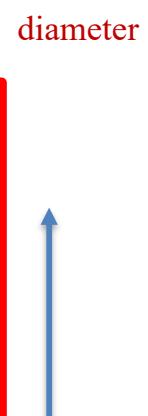


Adiabatic parcel simulations

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Larger values in observations (but instrumental uncertainty).  
Opposite trends in observations and adiabatic parcel simulations?

# Adiabatic parcel simulations with different updrafts: larger widths in polluted cases

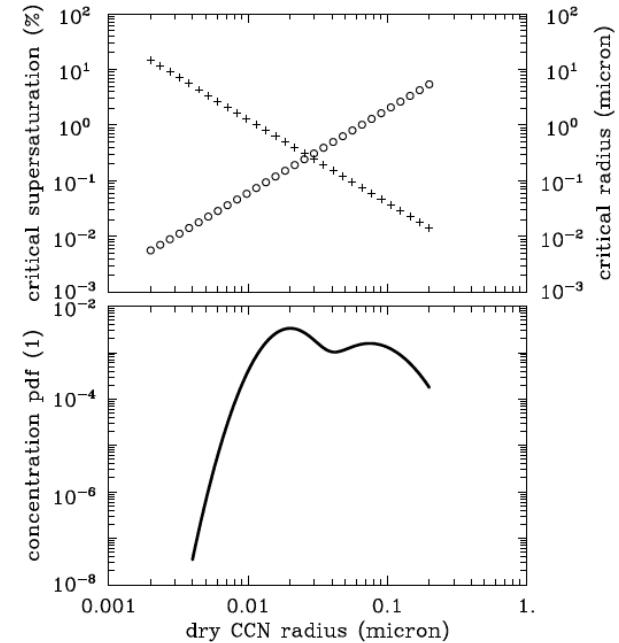
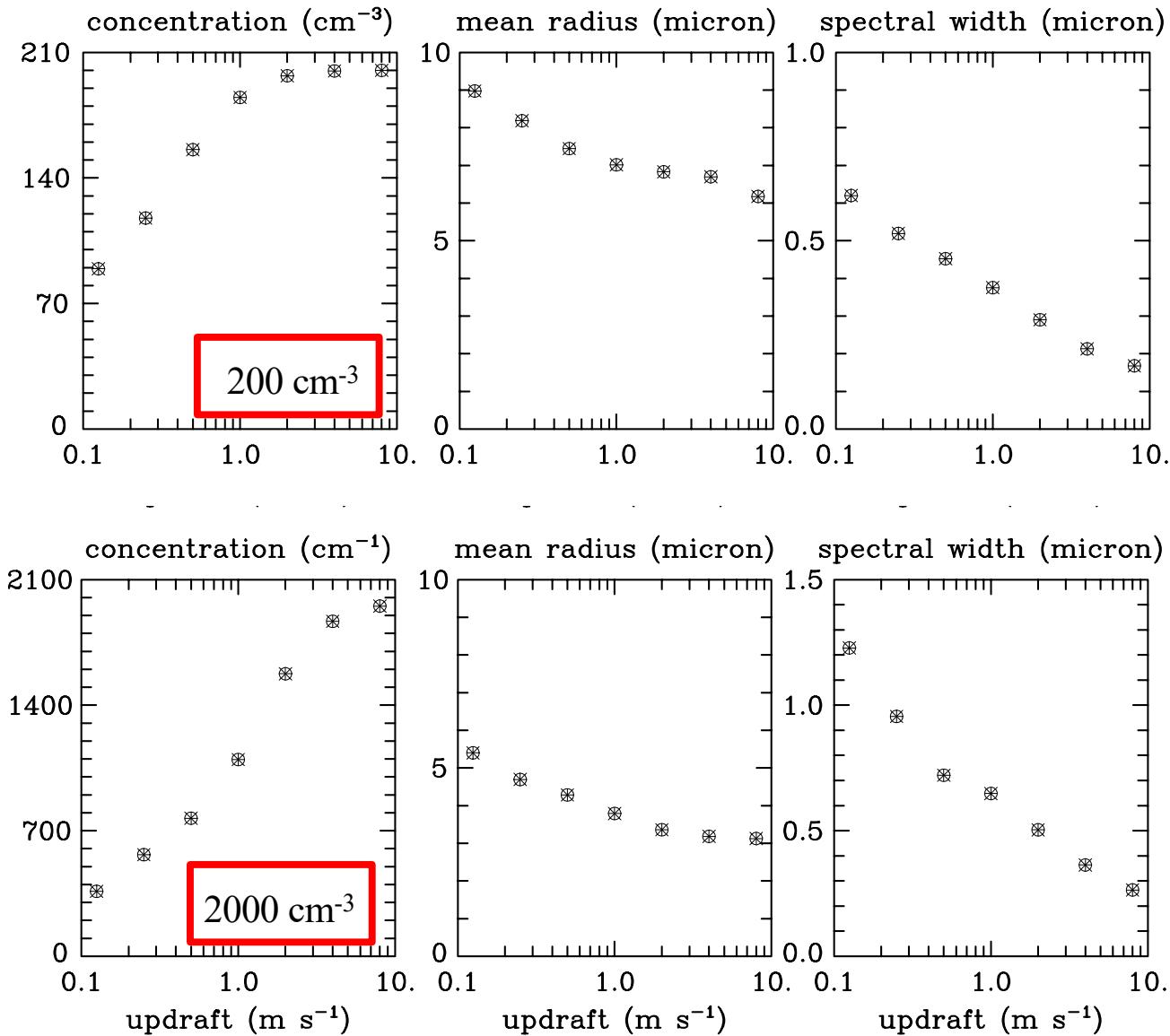
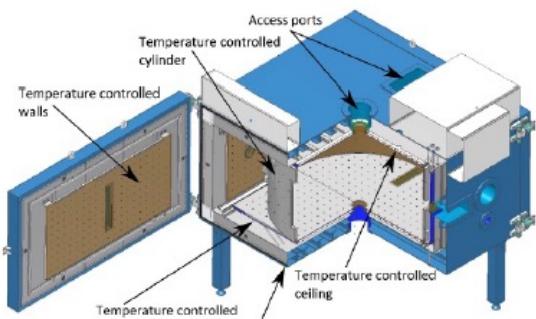


FIG. 2. (bottom) CCN distribution applied in simulations described in this paper. The distribution is not shown down to 2 nm ( $0.002 \mu\text{m}$ ) as the values are smaller than the lowest value on the vertical axis. (top) Critical (activation) supersaturation (plus symbols) and critical (activation) radius (circles) as a function of the CCN dry radius. Horizontal scale is as in the bottom panel.

# Pi chamber (Michigan Tech. U.) observations and simulations



$\dot{n}_a, \text{cm}^{-3} \text{ min}^{-1}$	$n_{a,int}, \text{cm}^{-3}$	$n, \text{cm}^{-3}$	$\bar{d}, \mu\text{m}$	diameter $\sigma_d, \mu\text{m}$
1	2	21.3	16.6	6.7
2	10	76.9	15.1	5.7
4	36	201.2	12.7	4.5
12	372	564.6	8.6	2.4
1,515	22,000	1,944.3	7.6	2.1

Observations: [Chandrakar et al. Proc. Nat. Ac. Sci. 2016](#): monodisperse dry CCN

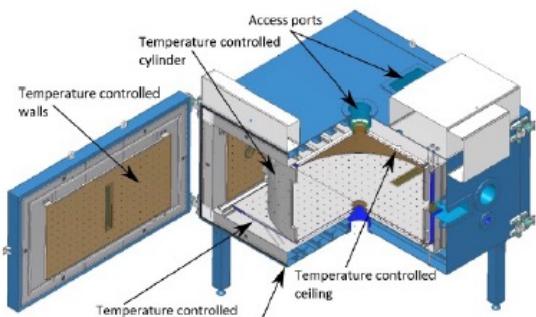
TABLE 1. Cloud water mixing ratio including all droplets ( $q_c$ ) and its mean spatial distribution standard deviation (in parentheses), TKE, mean droplet concentration, mean radius, and mean spectral width (the last three derived including only droplets with radius larger than the critical for each CCN bin) averaged over the last 10 min of model simulations.

	$q_c$ (std dev) (mg kg $^{-1}$ )	TKE (10 $^{-3}$ m $^2$ s $^{-2}$ )	Concentration (cm $^{-3}$ )	Radius ( $\mu\text{m}$ )	Spectral width ( $\mu\text{m}$ )	radius
C40	50.4 (34.8)	2.85	30.5	5.7	3.1	
C200	60.1 (47.3)	3.07	107	4.0	2.1	
C1000	53.8 (52.8)	3.23	300	2.6	1.4	
CROK	39.6 (44.5)	3.32	1330	1.3	0.7	

Simulations: [Grabowski et al. J. Atmos. Sci. 2024](#): dry CCN distributions

Smaller widths in polluted cases in both observations and simulations: [the impact of turbulence?](#)

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Can small-scale cloud turbulence explain the width of the droplet spectra in undiluted cloudy volumes?

# Can small-scale cloud turbulence explain the width of the droplet spectra in undiluted cloudy volumes?

The two papers that started it all. Other followed...

## **Microscopic Approach to Cloud Droplet Growth by Condensation. Part I: Model Description and Results without Turbulence**

**JAS 2001**

P. A. VAILLANCOURT\* AND M. K. YAU

*Department of Atmospheric and Oceanic Sciences, McGill University, Montreal, Quebec, Canada*

W. W. GRABOWSKI

*National Center for Atmospheric Research, Boulder, Colorado*

## **Microscopic Approach to Cloud Droplet Growth by Condensation. Part II: Turbulence, Clustering, and Condensational Growth**

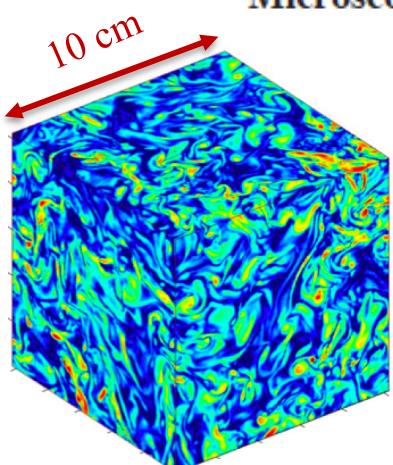
**JAS 2002**

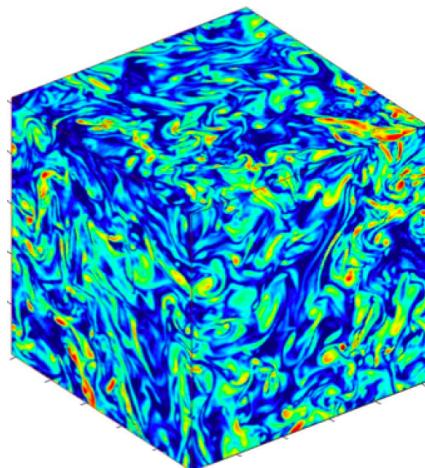
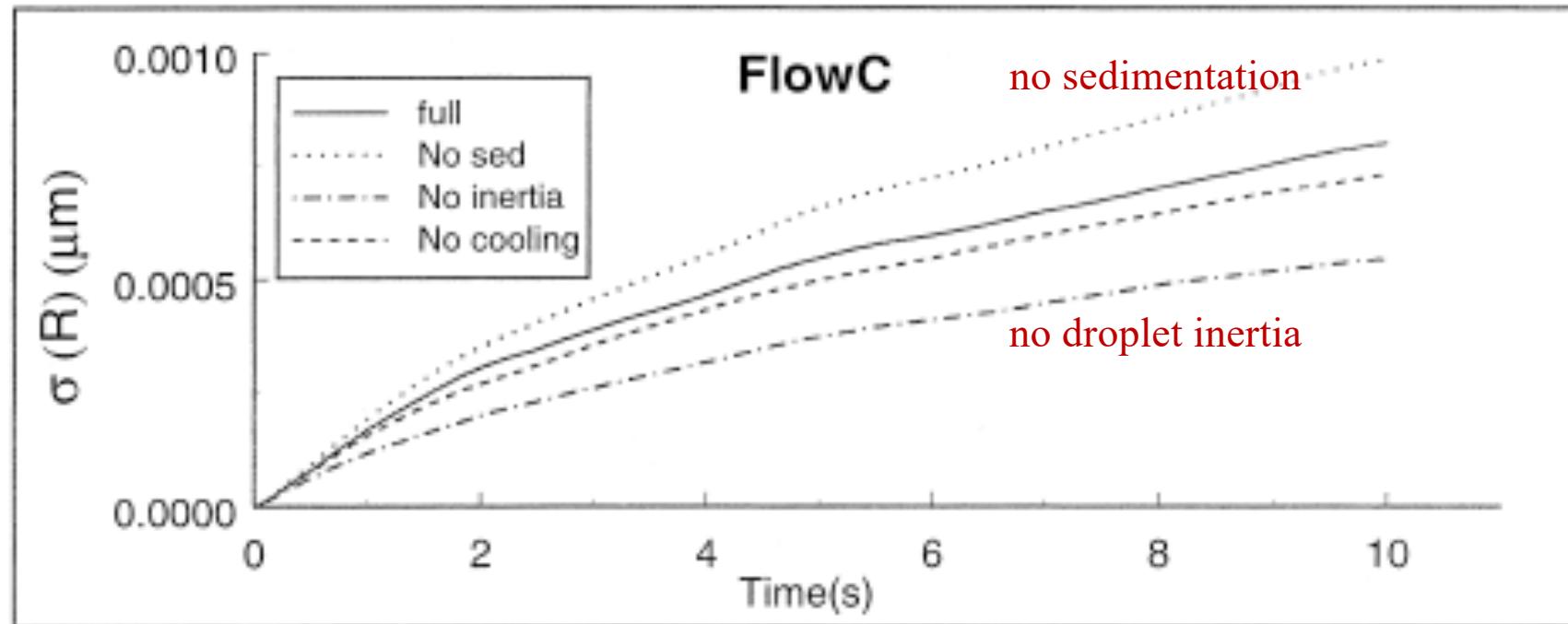
P. A. VAILLANCOURT, M. K. YAU, AND P. BARTELLO

*McGill University, Montréal, Québec, Canada*

W. W. GRABOWSKI

*National Center for Atmospheric Research, Boulder, Colorado*





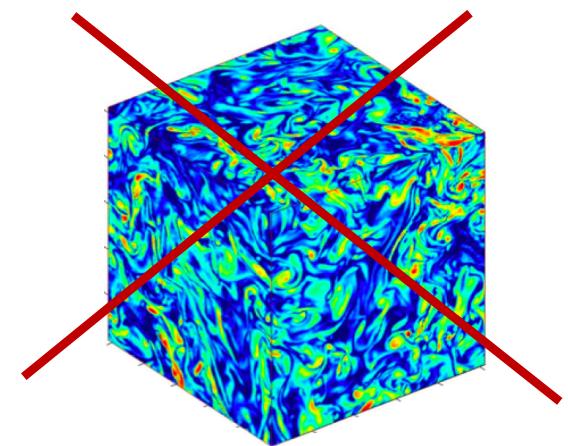
Several subsequent studies  
pursued this line of research...  
(see a review in Grabowski *JAS* 2025)

Vaillancourt et al. *JAS* 2002

## Broadening of Cloud Droplet Spectra through Eddy Hopping: Why Did We All Have It Wrong?

WOJCIECH W. GRABOWSKI<sup>a</sup>

<sup>a</sup> *NSF NCAR, Boulder, Colorado*

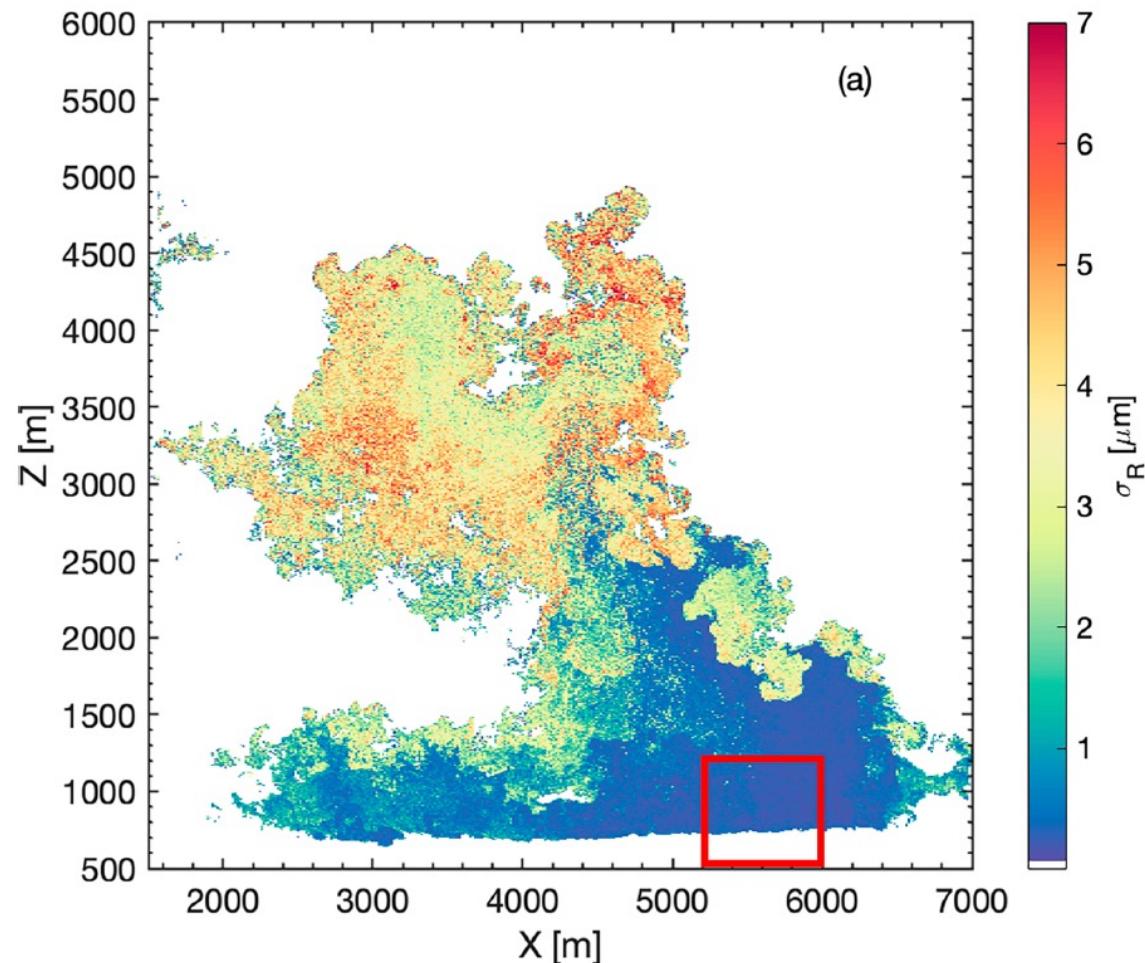


DNS-type studies do not really help understanding broadening droplet spectra in adiabatic volumes of natural clouds...

## Untangling the Broadening of Adiabatic Cloud Droplet Spectra through Eddy Hopping in a High-Resolution Cumulus Congestus Simulation

WOJCIECH W. GRABOWSKI,<sup>a</sup> KAMAL KANT CHANDRAKAR,<sup>a</sup> AND HUGH MORRISON<sup>a</sup>

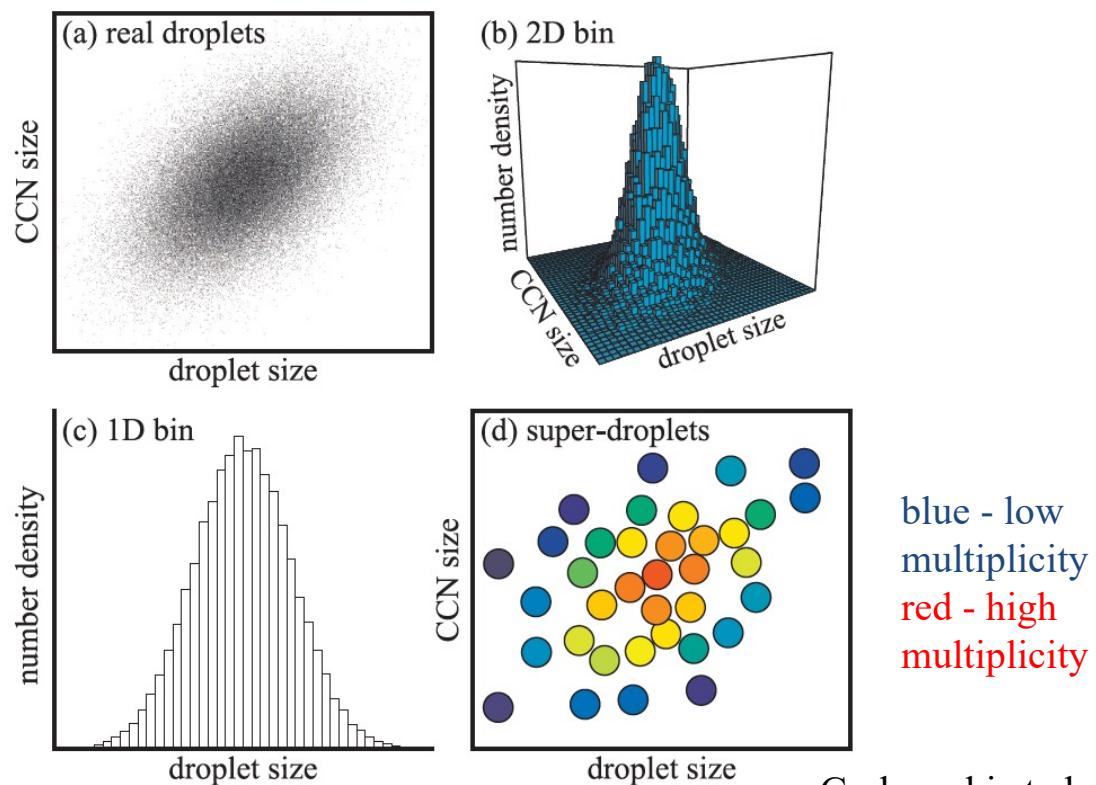
<sup>a</sup> MMM Laboratory, NSF National Center for Atmospheric Research, Boulder, Colorado



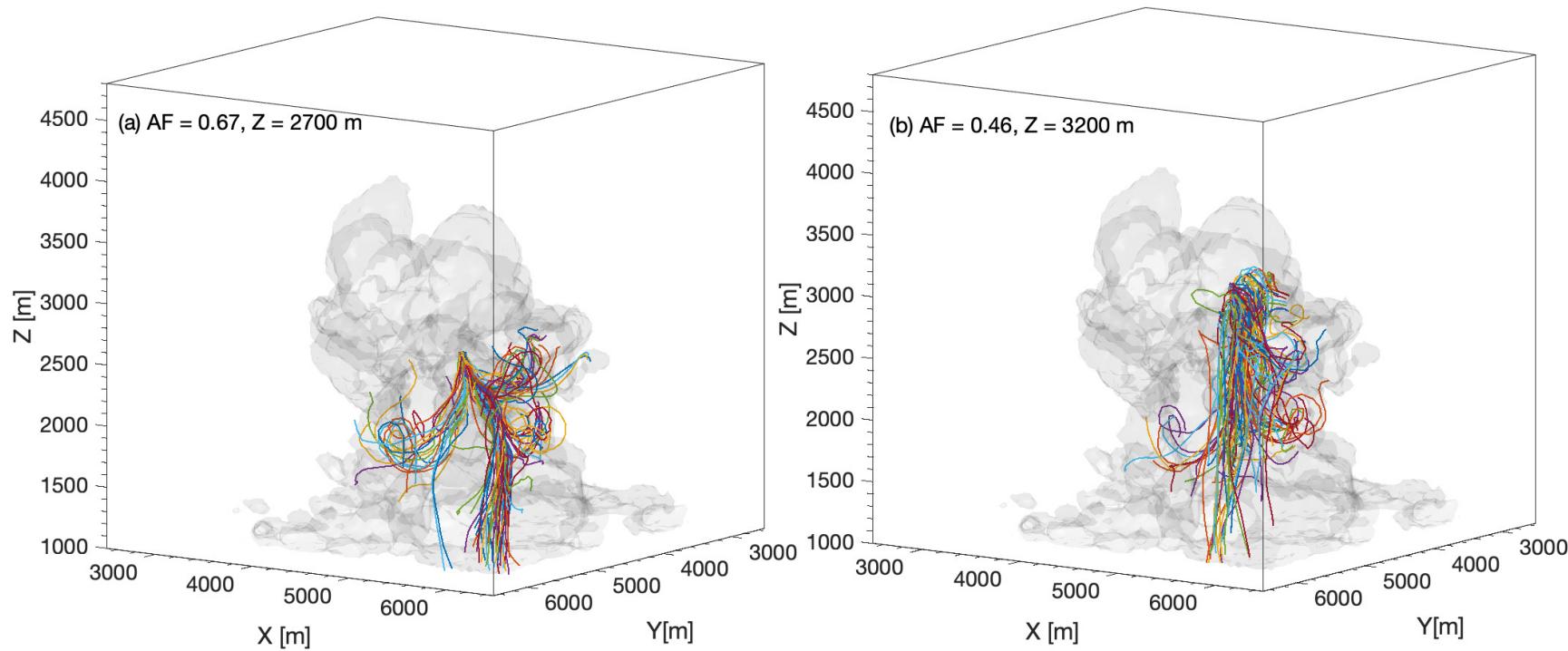
Lasher-Trapp et al. (2005) used an elaborate scheme to calculate individual droplet growth along their trajectories through a turbulent cloud.

This is **not needed** when cloud model applies Lagrangian particle-based microphysics because each superdroplet follows its own trajectory.

However, high spatial resolution is needed to appropriately simulate the impact of cloud turbulence on the droplet growth.



# 3D cloud simulations applying Lagrangian particle-base methodology, the superdroplet method (Shima et al.)

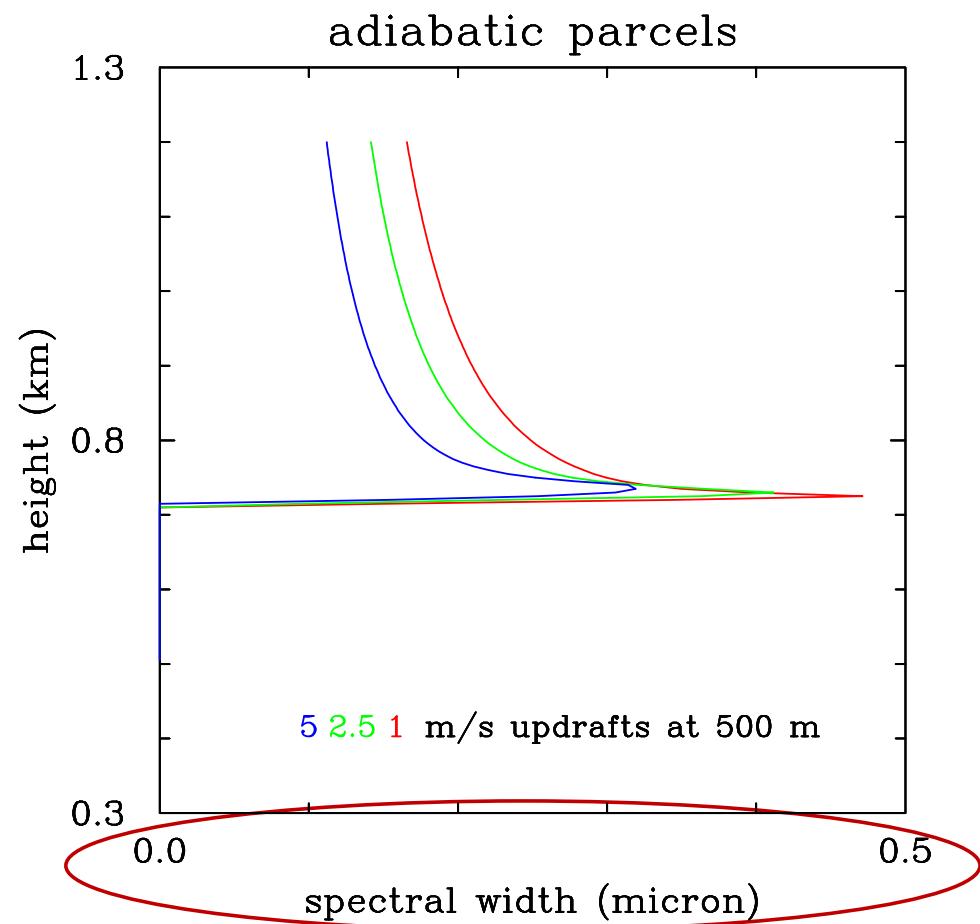
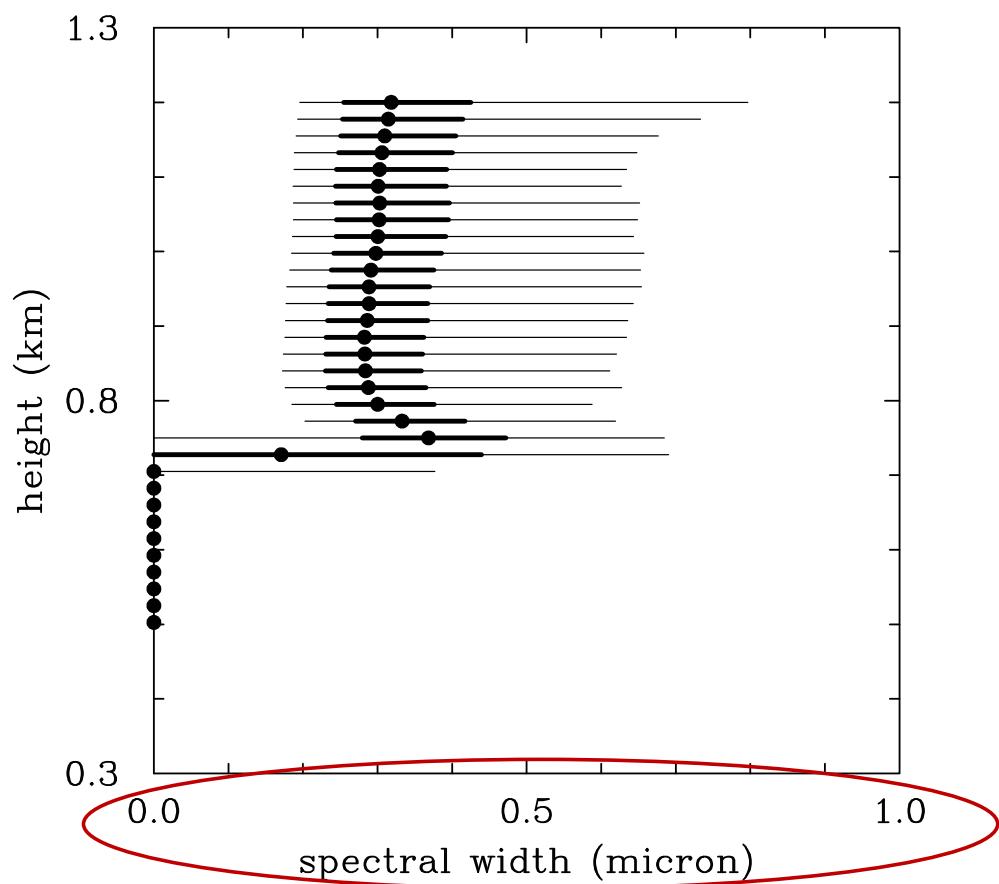


Chandrakar et al. *JAS* 2021

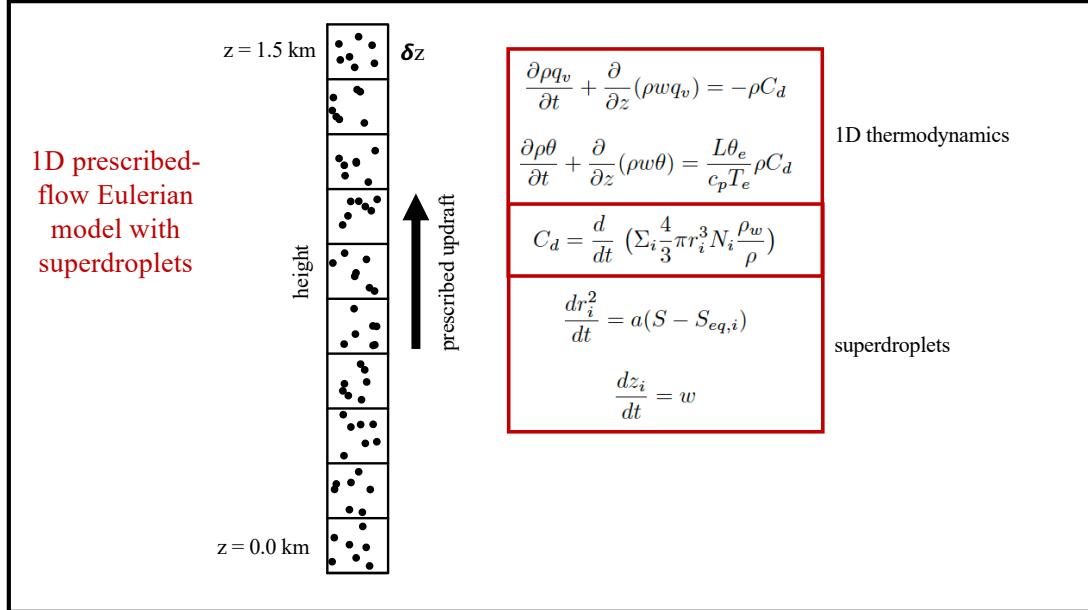
Trajectories of selected “super-droplets” arriving at a given location (different in right and left panels) above the cloud base. Example of “eddy hopping” at the cloud scale...

Can “eddy hopping” in a turbulent cloud lead to the spectral width increase even if there is no cloud dilution (i.e., adiabatic fraction close to 1)?

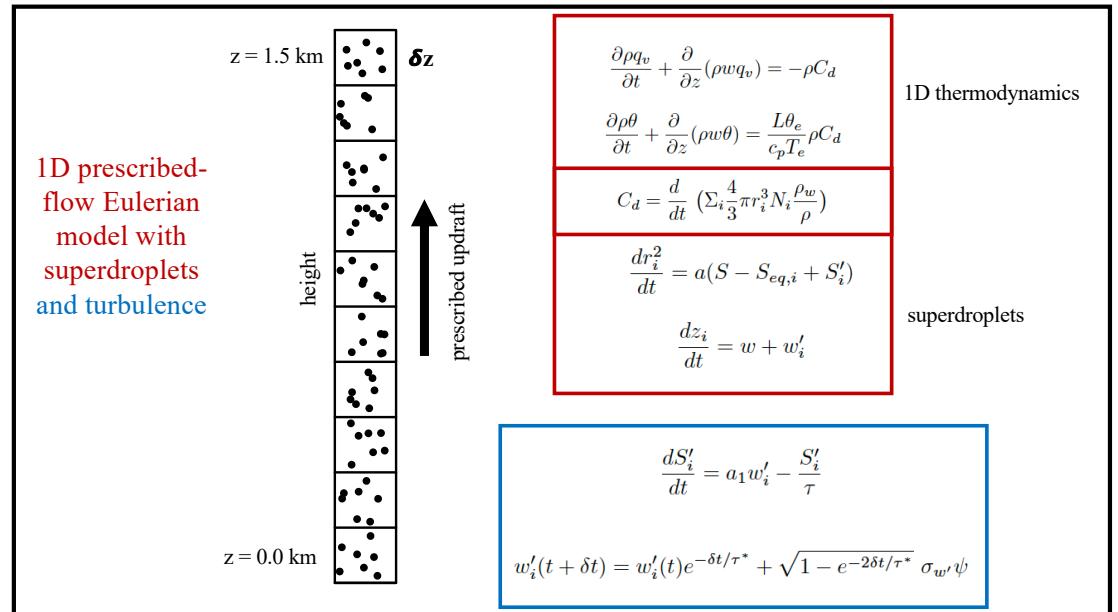
# Adiabatic droplet spectra in 3D cloud simulation with polluted dry CCN distributions versus adiabatic parcels:



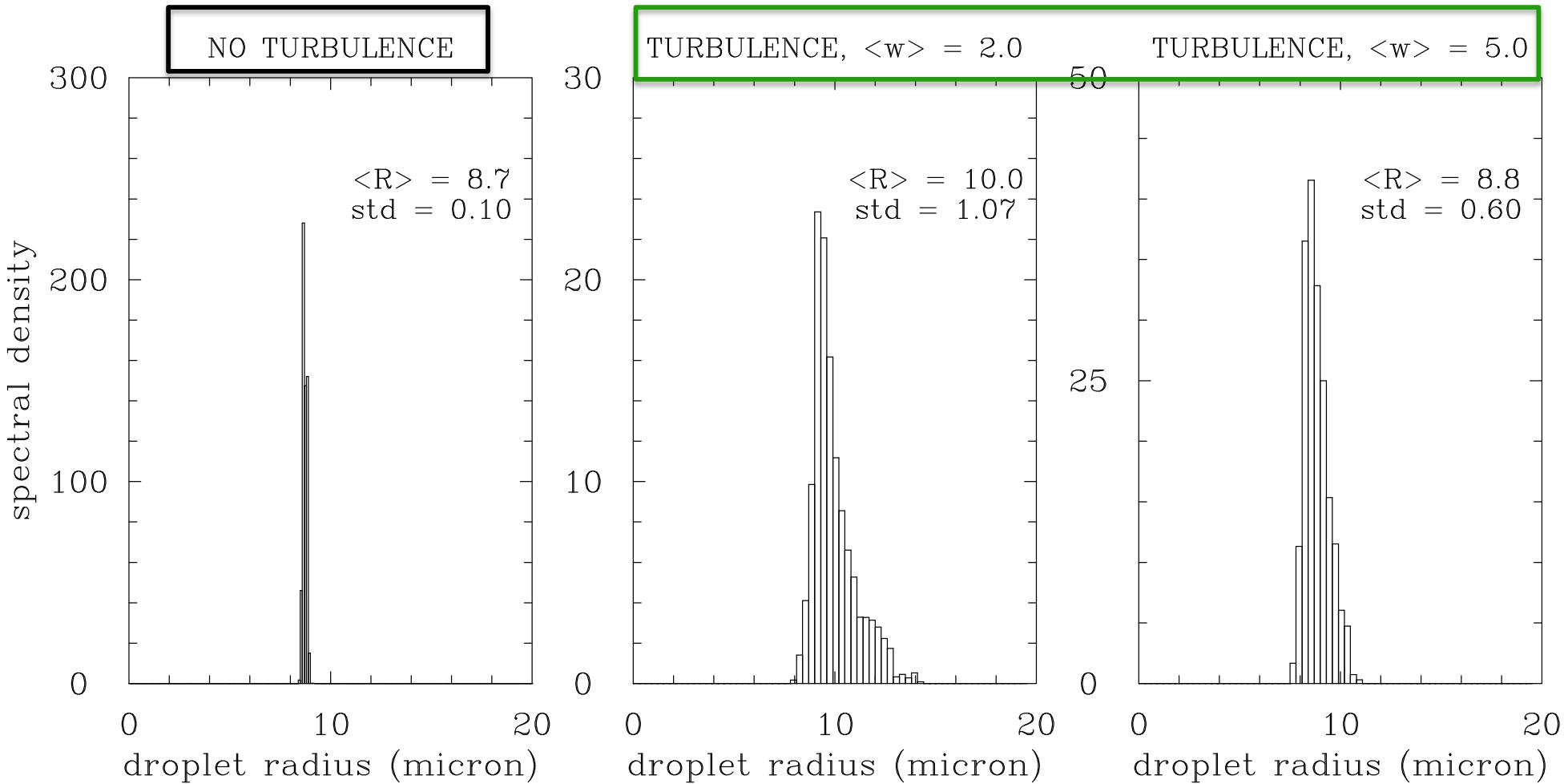
No turbulence: each superdroplet grows in exactly the same supersaturation  $S$



With turbulence: in addition to mean  $S$ , each superdroplet experiences turbulence-driven  $S'$



# Spectra at 1.5 km height from 1D Eulerian-Lagrangian simulations without and with effects of cloud turbulence (based on 3D simulation conditions).



Using the 1D Eulerian-Lagrangian framework, we address two questions:

How to understand larger spectral widths in observations  
when compared to adiabatic parcel simulations?

How to understand what seems to be opposite polluted vs pristine  
trends in observations and adiabatic parcel simulations?

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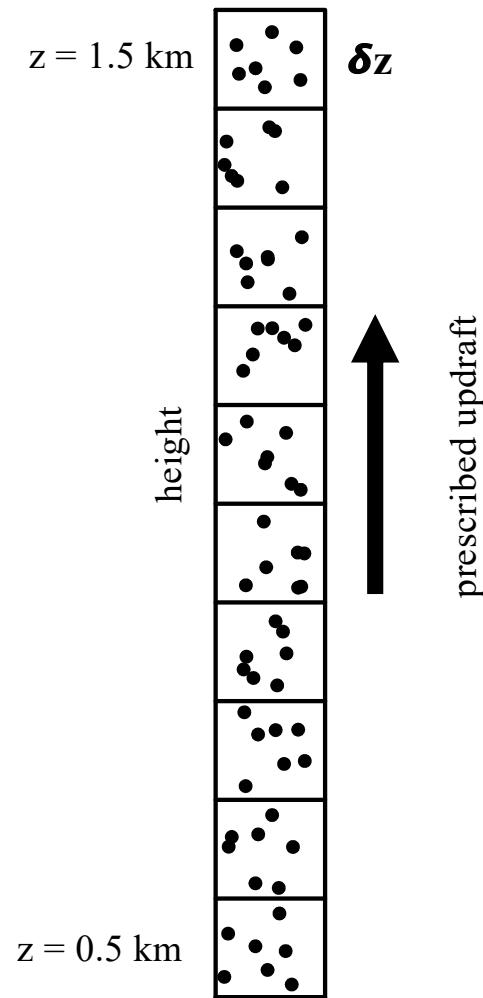
How to understand what seems to be opposite polluted vs pristine  
trends in observations and adiabatic parcel simulations?

The answer to both questions:

*Impact of cloud turbulence on formation and growth of cloud droplets!*

No turbulence:

1D prescribed-flow Eulerian model with superdroplets



$$\frac{\partial \rho q_v}{\partial t} + \frac{\partial}{\partial z} (\rho w q_v) = -\rho C_d$$

$$\frac{\partial \rho \theta}{\partial t} + \frac{\partial}{\partial z} (\rho w \theta) = \frac{L \theta_e}{c_p T_e} \rho C_d$$

$$C_d = \frac{d}{dt} \left( \sum_i \frac{4}{3} \pi r_i^3 N_i \frac{\rho_w}{\rho} \right)$$

$$\frac{dr_i^2}{dt} = a(S - S_{eq,i})$$

$$\frac{dz_i}{dt} = w$$

1D thermodynamics

superdroplets

## No turbulence:

1.5 km deep 1D domain, 300 grid points, constant updraft of 1, 2, and 4 m s<sup>-1</sup>  
 $dz = 5$  m,  $dt = 0.1$  sec (sub-stepping for droplet growth)

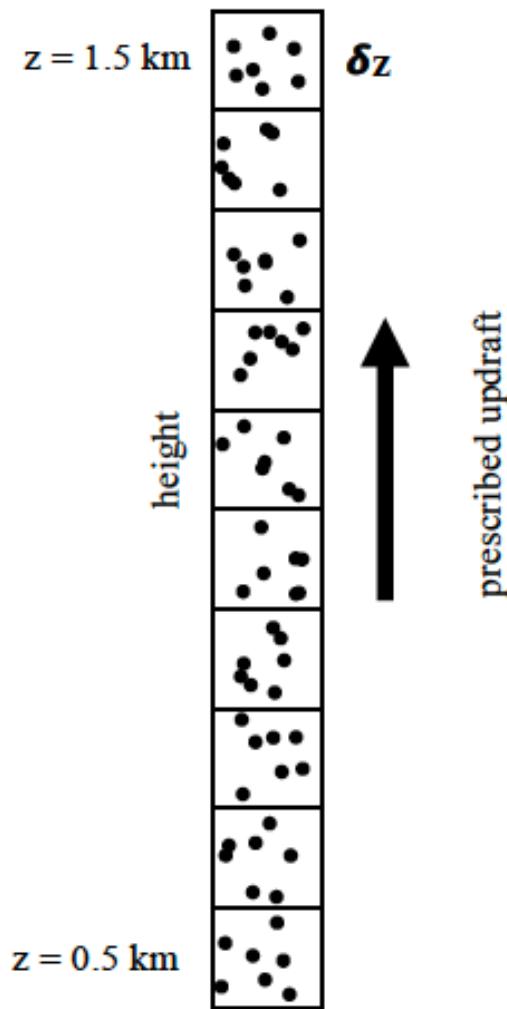
1D advection: MPDATA scheme (Smolarkiewicz et al.)  
inflow – constant in time  
outflow – unimportant

## Superdroplets (SDs):

- 100 CCN bins (5-500 nm), each bin with 32 SDs per grid volume (total 963,200 SDs)
  - SDs randomly positioned at onset with initial radius at equilibrium with local supersaturation
    - SDs advected with the mean updraft
- SDs moved to the bottom grid volume when leaving top of the domain with radius reset to the initial radius
- all SDs within a given grid volume grow in the same supersaturation  $S(q_v, T)$

# With turbulence:

1D prescribed-flow Eulerian model with superdroplets and turbulence



$$w'_i(t + \delta t) = w'_i(t) e^{-\delta t/\tau^*} + \sqrt{1 - e^{-2\delta t/\tau^*}} \sigma_{w'} \psi$$

$$\frac{\partial \rho q_v}{\partial t} + \frac{\partial}{\partial z} (\rho w q_v) = -\rho C_d$$

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$$\frac{dr_i^2}{dt} = a(S - S_{eq,i} + S'_i)$$

$$\frac{dz_i}{dt} = w + w'_i$$

1D thermodynamics

superdroplets

$$\frac{dS'_i}{dt} = a_1 w'_i - \frac{S'_i}{\tau}$$

$w'$ ,  $S'$  – turbulence!

## Adding turbulence:

Each SD grows in the supersaturation that comes from the combination of the mean  $S(q_v, T)$  and fluctuations  $S'$  driven by the stochastic model

Stochastic model parameters similar to 3D cloud simulation:

mean TKE dissipation  $\epsilon = 10 \text{ cm}^2 \text{ s}^{-3}$

$L$  (integral length scale): 240 m

Height-dependent phase relaxation time  $\tau$  the same for all SDs  
(derived from turbulence-free simulation)

vertical velocity standard deviation  $\sim 0.5 \text{ m s}^{-1}$

turbulence integral time scale  $\tau^* \sim 240 \text{ s}$

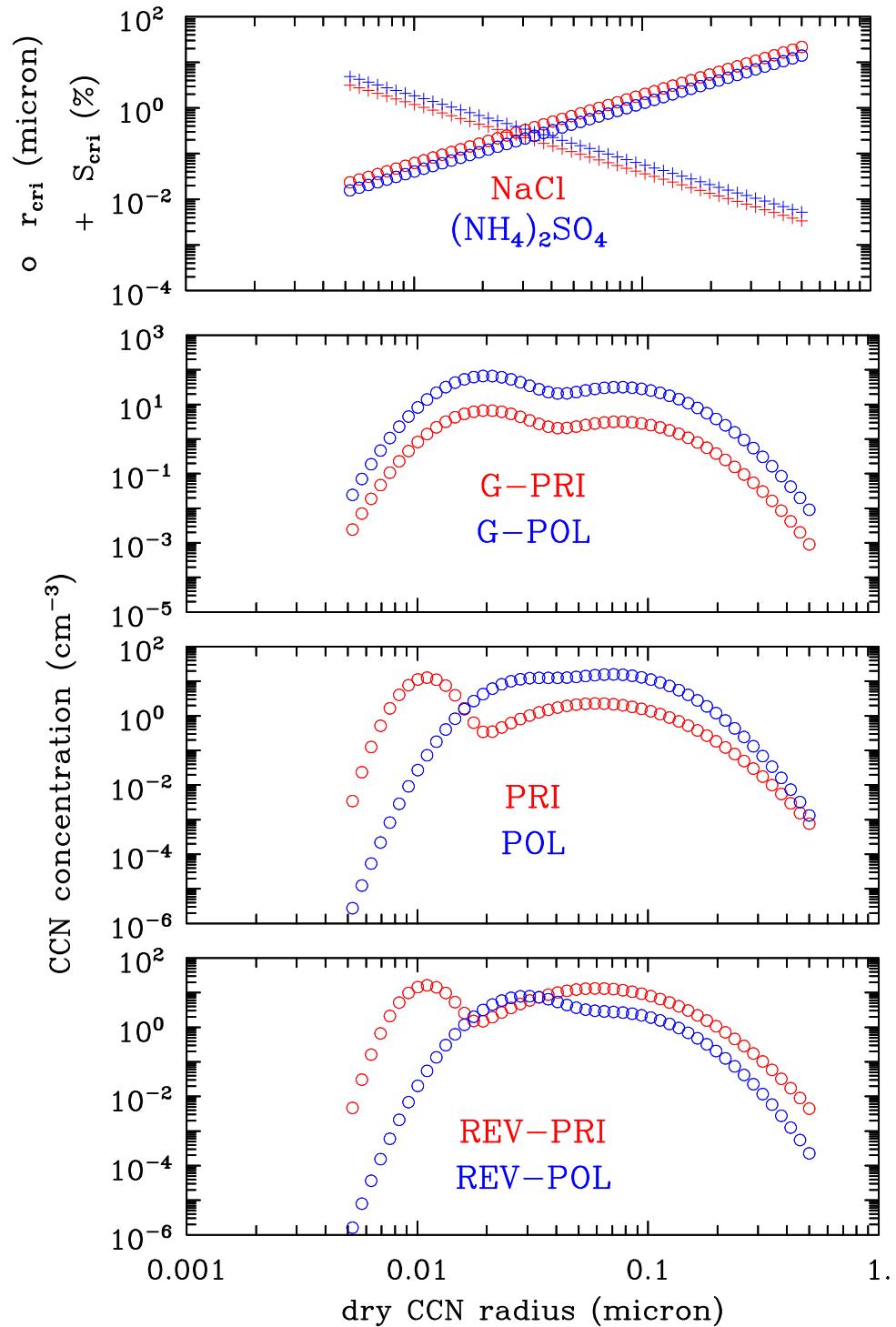
the same for all simulations

## Bimodal dry CCN distributions: pristine versus polluted

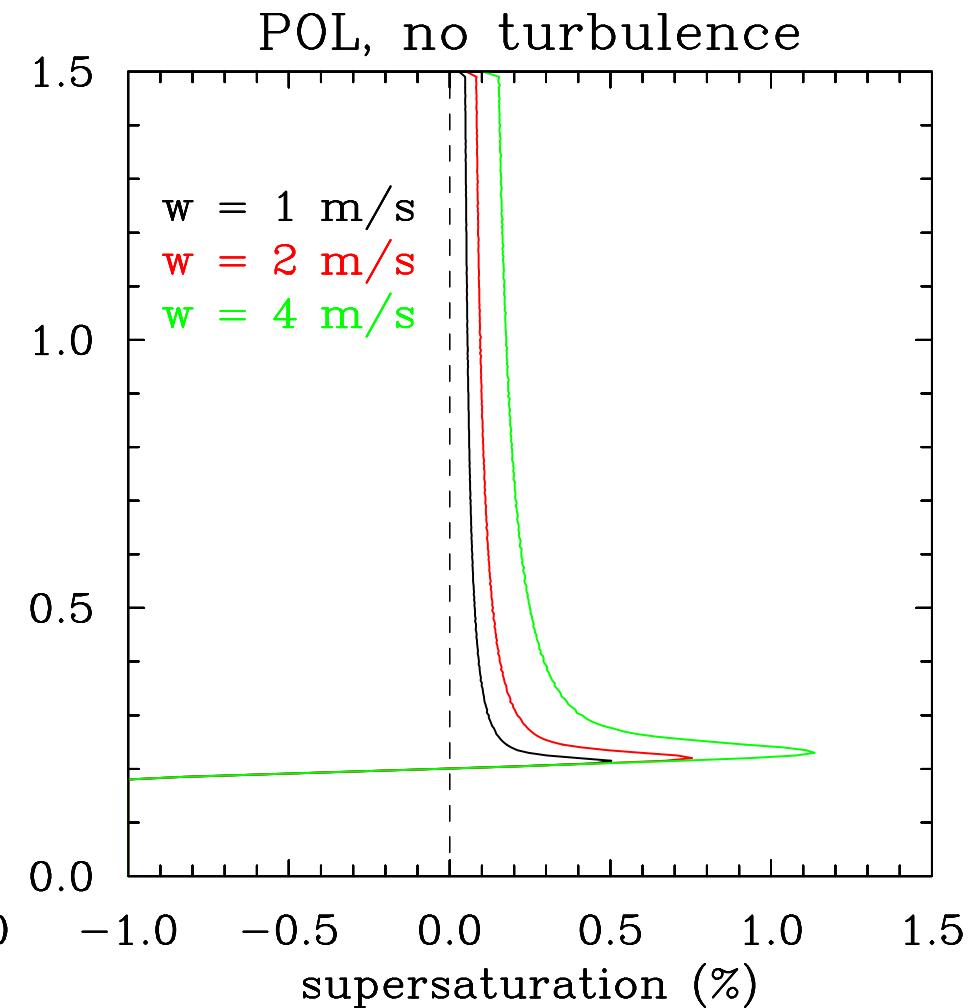
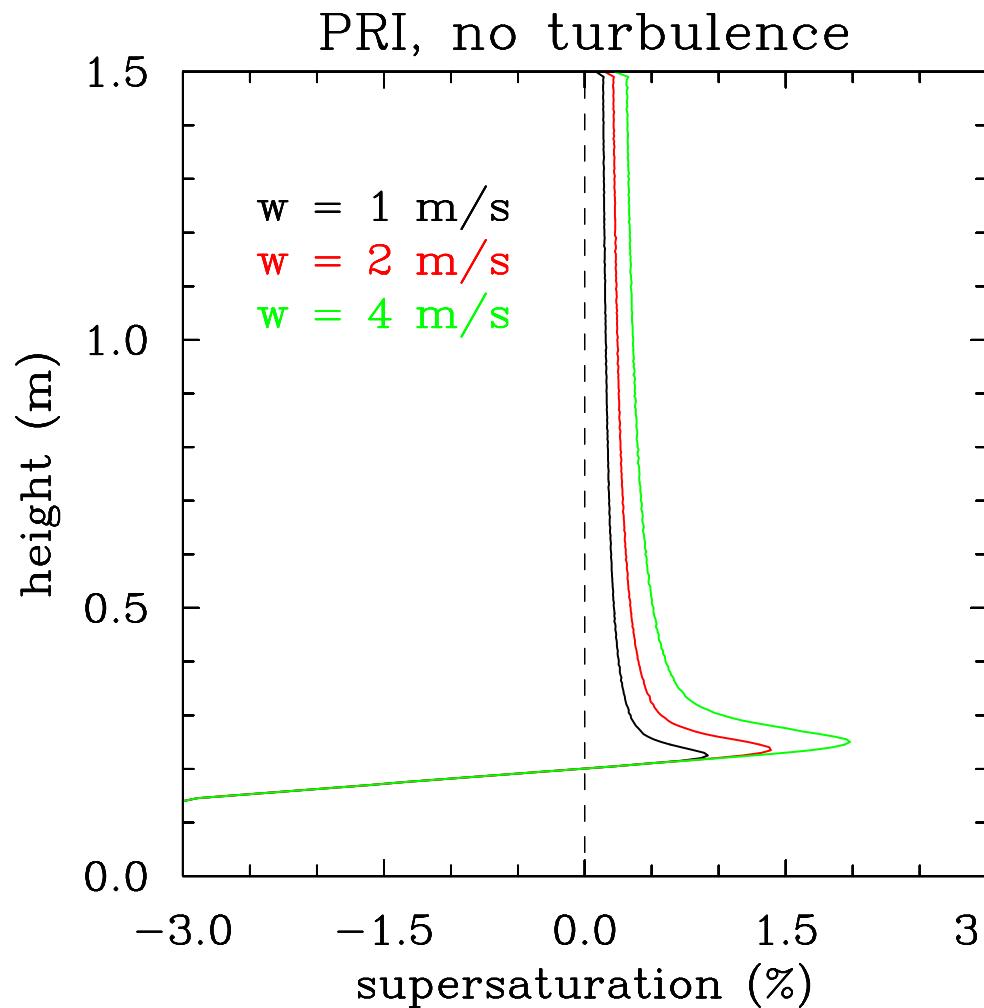
CCN distribution	Reference	Comments
POL	Grabowski et al. 2011, Grabowski and Pawlowska 2023	Polluted CCN from VOCALS field project
PRI	Grabowski et al. 2011, Grabowski and Pawlowska 2023	Clean CCN from DYCOMS field project
REV-POL	Grabowski and Pawlowska 2023 (supporting information)	CCN spectral shape of POL with N <sub>1</sub> and N <sub>2</sub> concentrations from PRI
REV-PRI	Grabowski and Pawlowska 2023 (supporting information)	CCN spectral shape of PRI with N <sub>1</sub> and N <sub>2</sub> concentrations from POL
G-POL	Arabas et al. 2015, Grabowski et al. 2022	Spectral shape similar to POL, polluted N <sub>1</sub> and N <sub>2</sub> concentrations
G-1000	Arabas et al. 2015, Grabowski et al. 2022	As G-POL, but 2 times smaller N <sub>1</sub> and N <sub>2</sub> concentrations
G-PRI	Arabas et al. 2015, Grabowski et al. 2022	As G-POL, but 10 times smaller N <sub>1</sub> and N <sub>2</sub> concentrations

CCN distribution	N <sub>1</sub> (cm <sup>-3</sup> )	r <sub>1</sub> (nm)	σ <sub>1</sub> (1)	N <sub>2</sub> (cm <sup>-3</sup> )	r <sub>2</sub> (nm)	σ <sub>2</sub> (1)	chemical composition
POL	160.	29.	1.36	380.	71.	1.57	(NH <sub>4</sub> ) <sub>2</sub> SO <sub>4</sub>
PRI	125	11.	1.20	65.	60.	1.70	NaCl
REV-POL	125.	29.	1.36	65.	71.	1.57	(NH <sub>4</sub> ) <sub>2</sub> SO <sub>4</sub>
REV-PRI	160.	11.	1.20	380.	60.	1.70	NaCl
G-POL	1,200.	20.	1.40	800.	75.	1.60	NaCl
G-1000	600.	20.	1.40	400.	75.	1.60	NaCl
G-PRI	120.	20.	1.40	80.	75.	1.60	NaCl

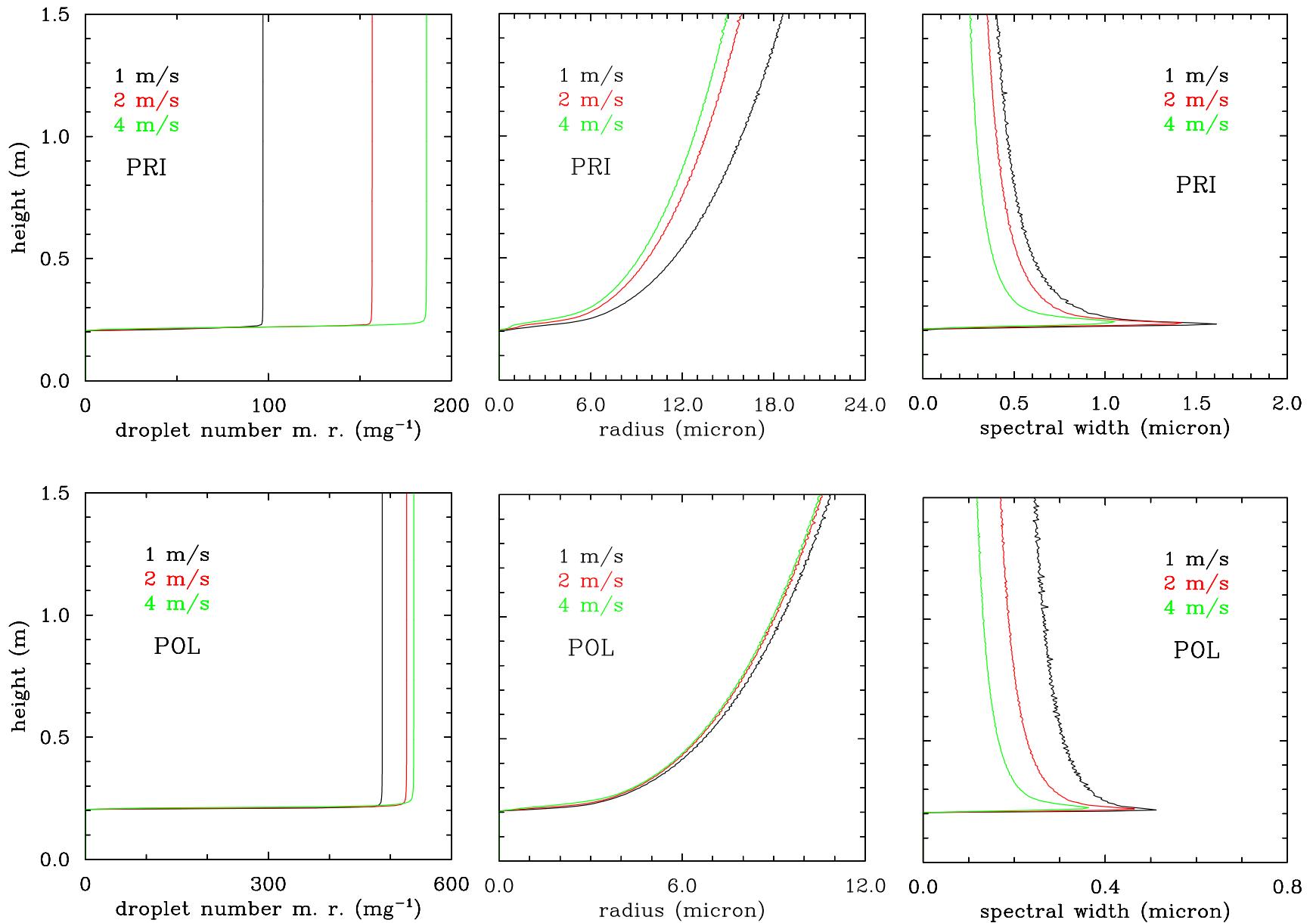
Dry CCN distributions:  
pristine  
versus  
polluted



## WITHOUT TURBULENCE

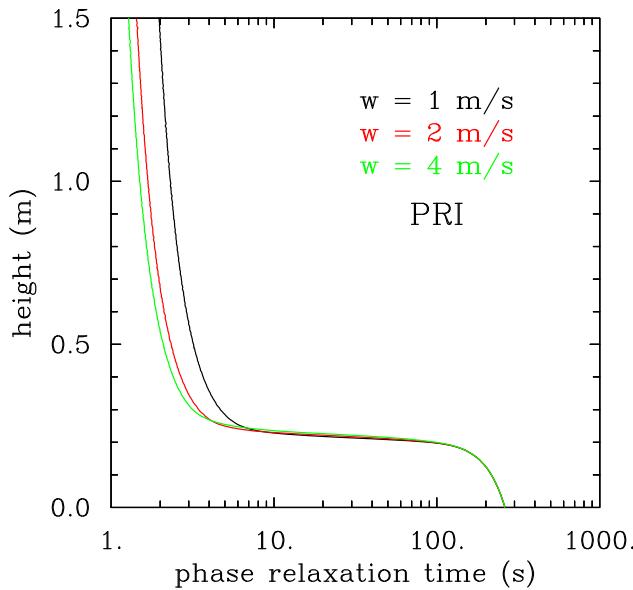


## WITHOUT TURBULENCE

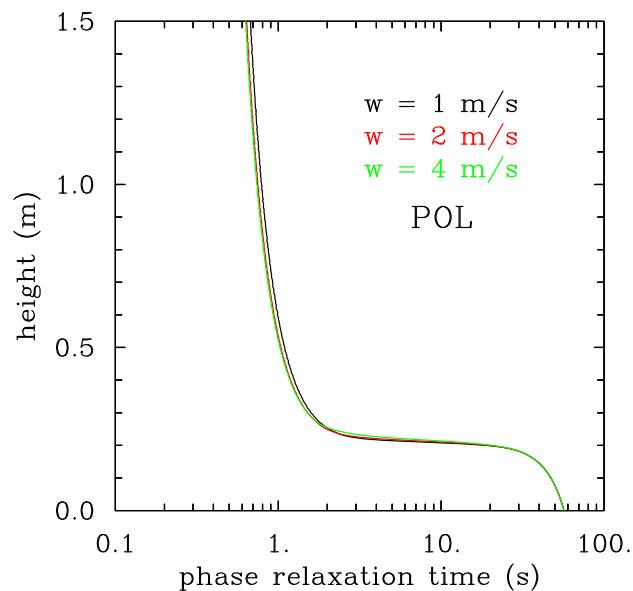


## ADDING TURBULENCE

we need information about the phase relaxation time

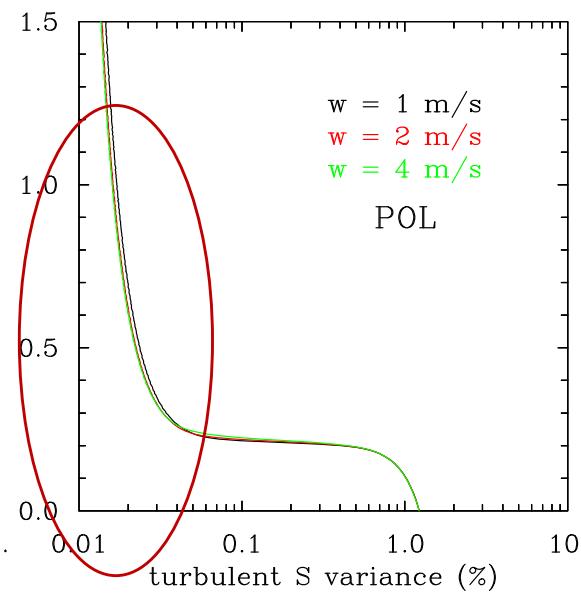
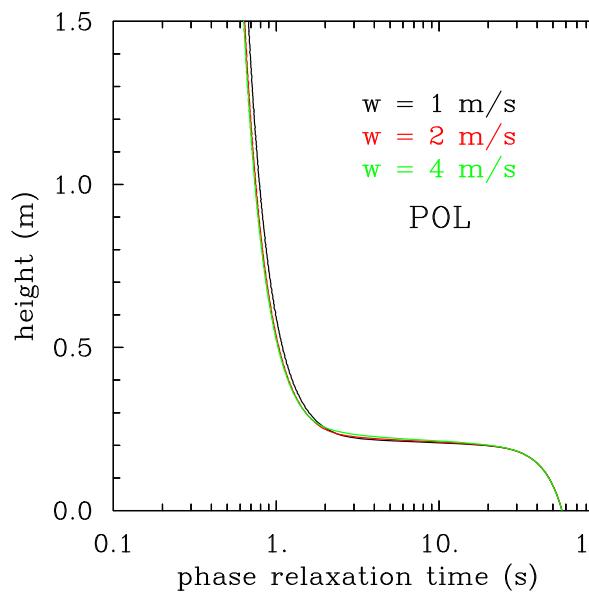
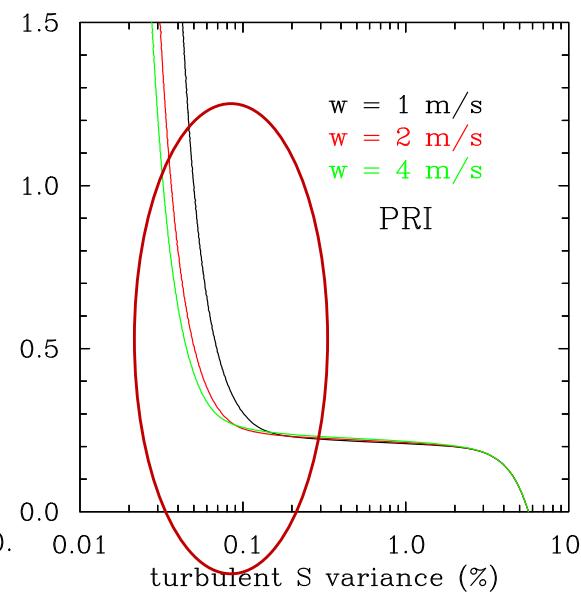
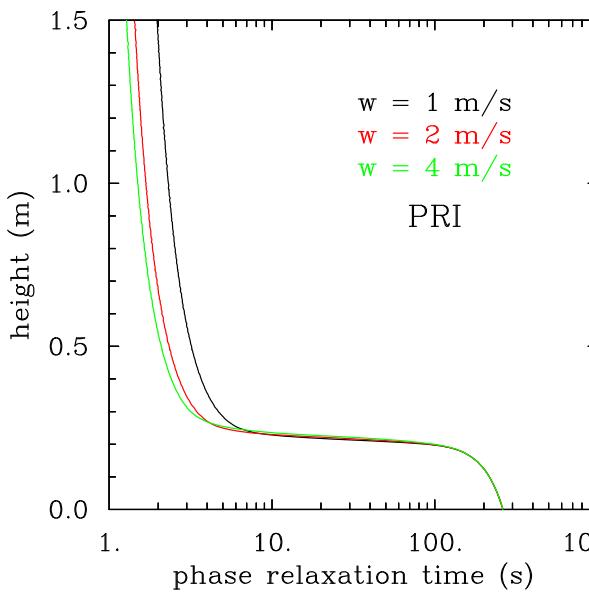


$$\frac{dS'_i}{dt} = a_1 w'_i - \frac{S'_i}{\tau}$$



## ADDING TURBULENCE

we need information about the phase relaxation time



$$\frac{dS'_i}{dt} = a_1 w'_i - \frac{S'_i}{\tau}$$

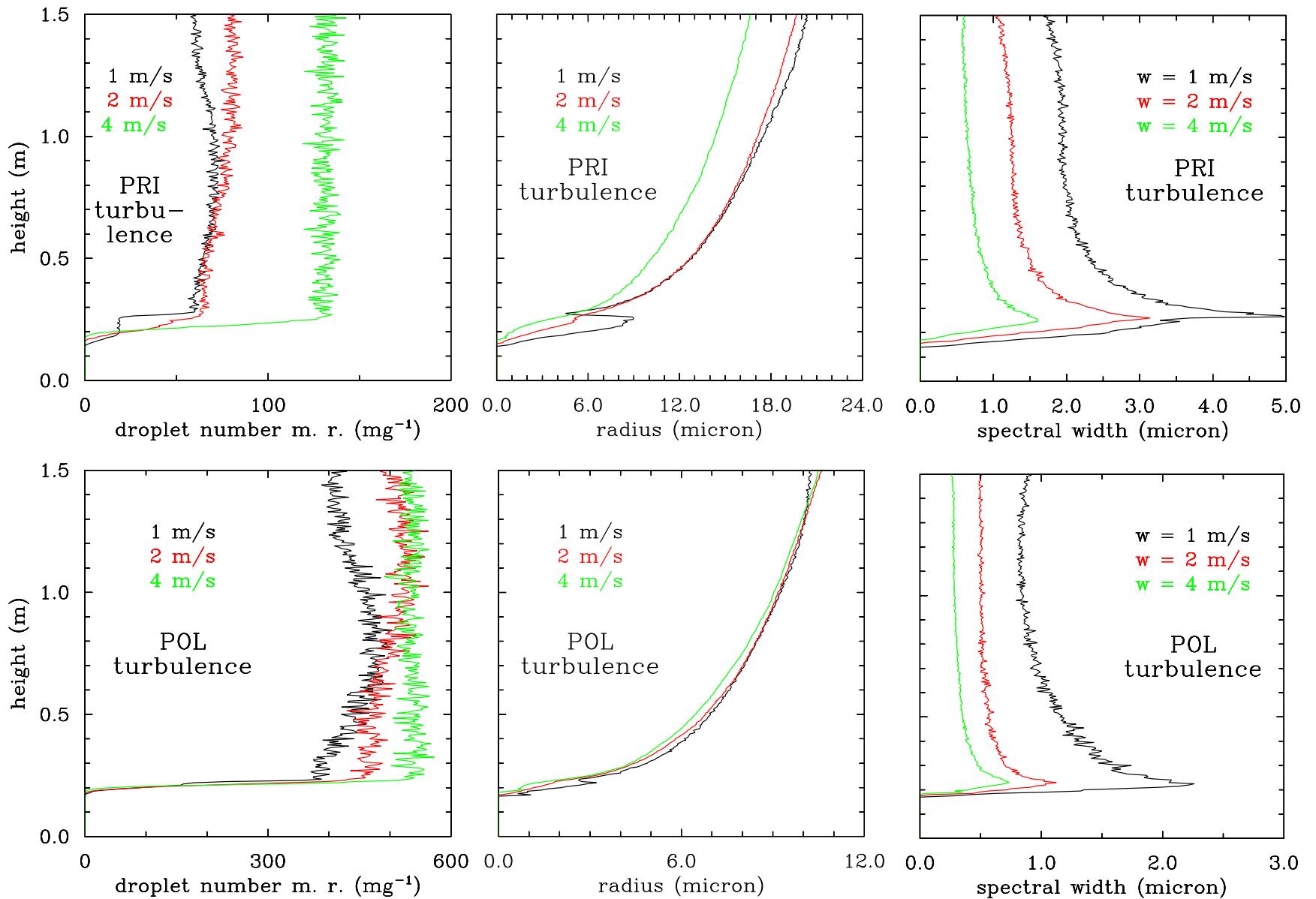
For the quasi-equilibrium supersaturation:

$$S_{qe} = a_1 \tau w$$

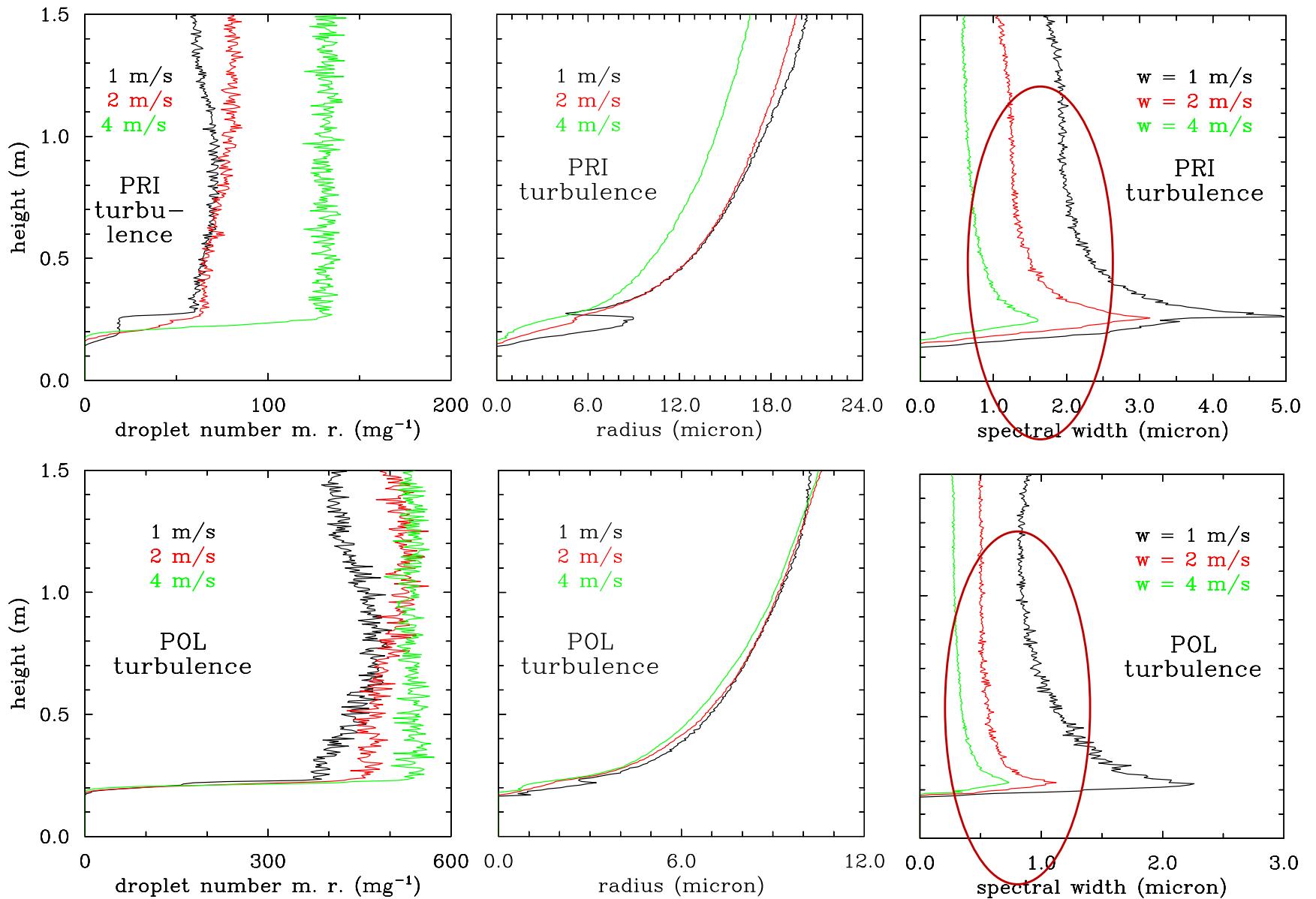
$$\sigma_S = a_1 \tau \sigma_w$$

$\sigma_w = 0.54 \text{ m sec}^{-1}$  is the vertical velocity standard deviation

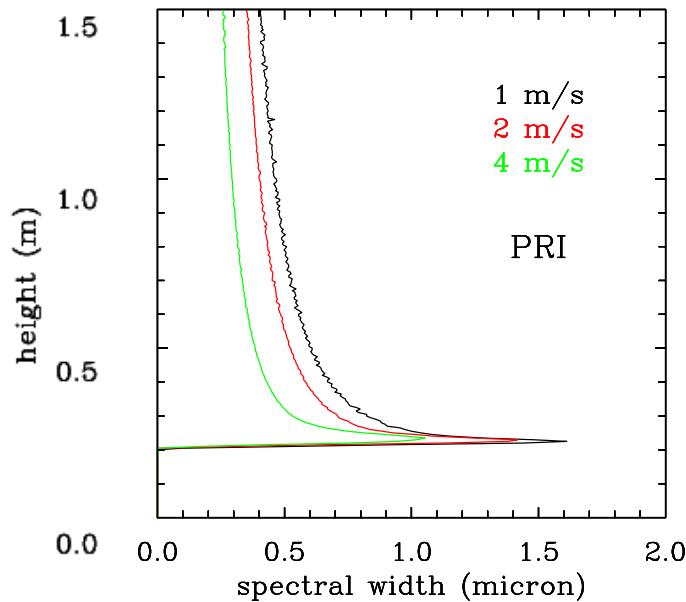
# WITH TURBULENCE



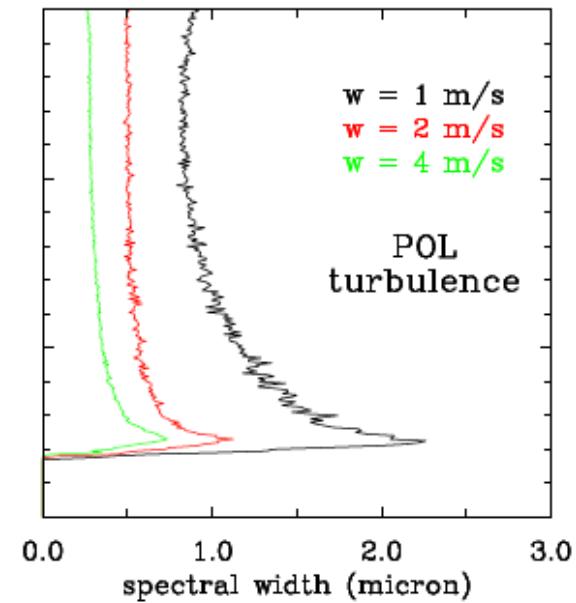
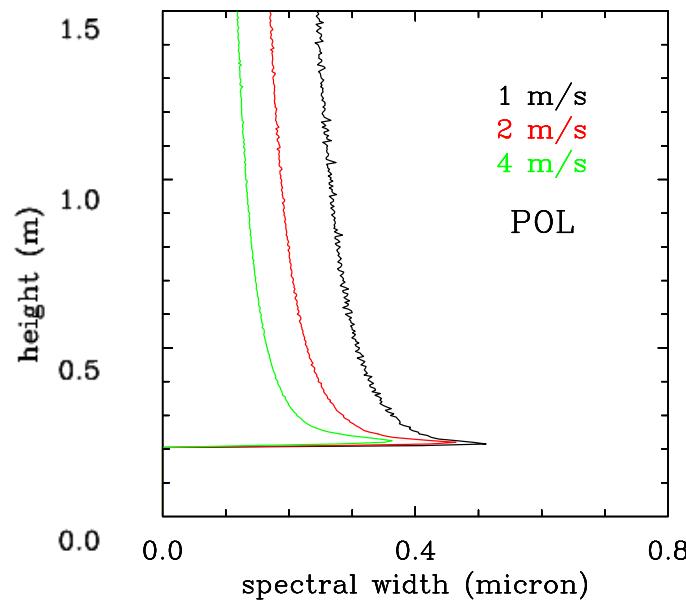
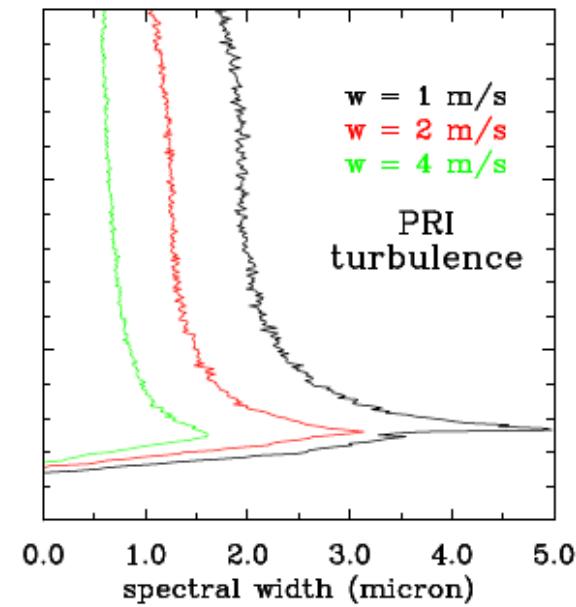
# WITH TURBULENCE



WITHOUT TURBULENCE



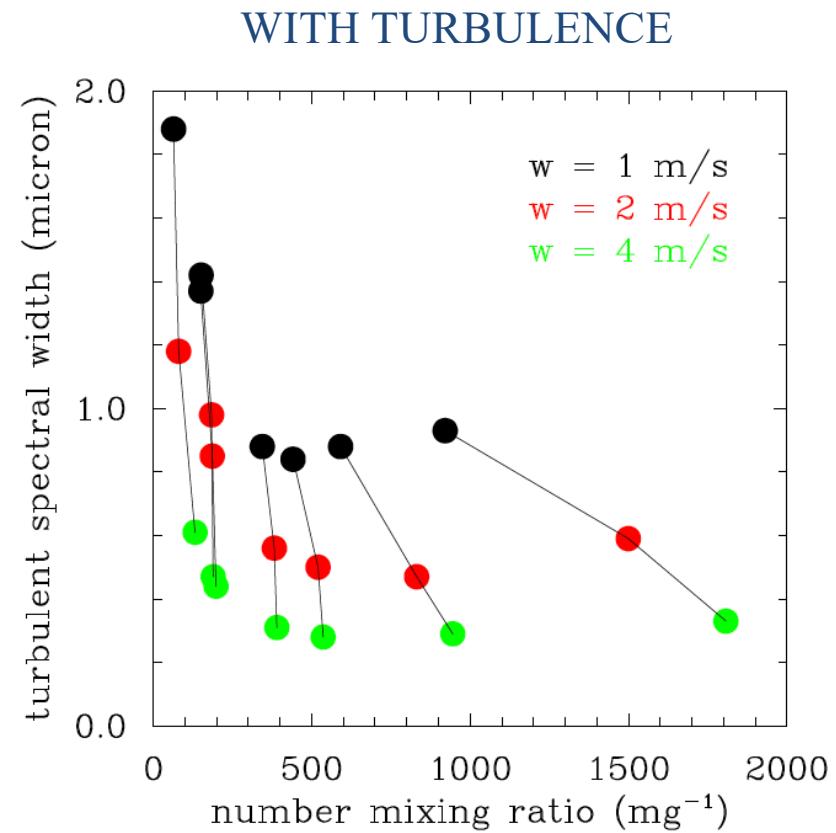
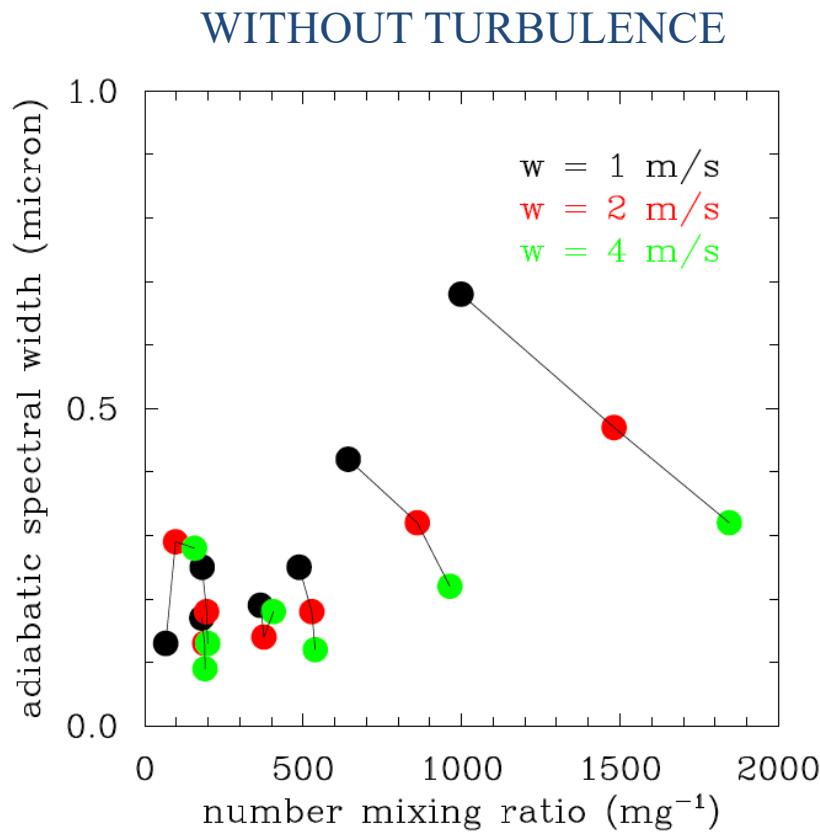
WITH TURBULENCE



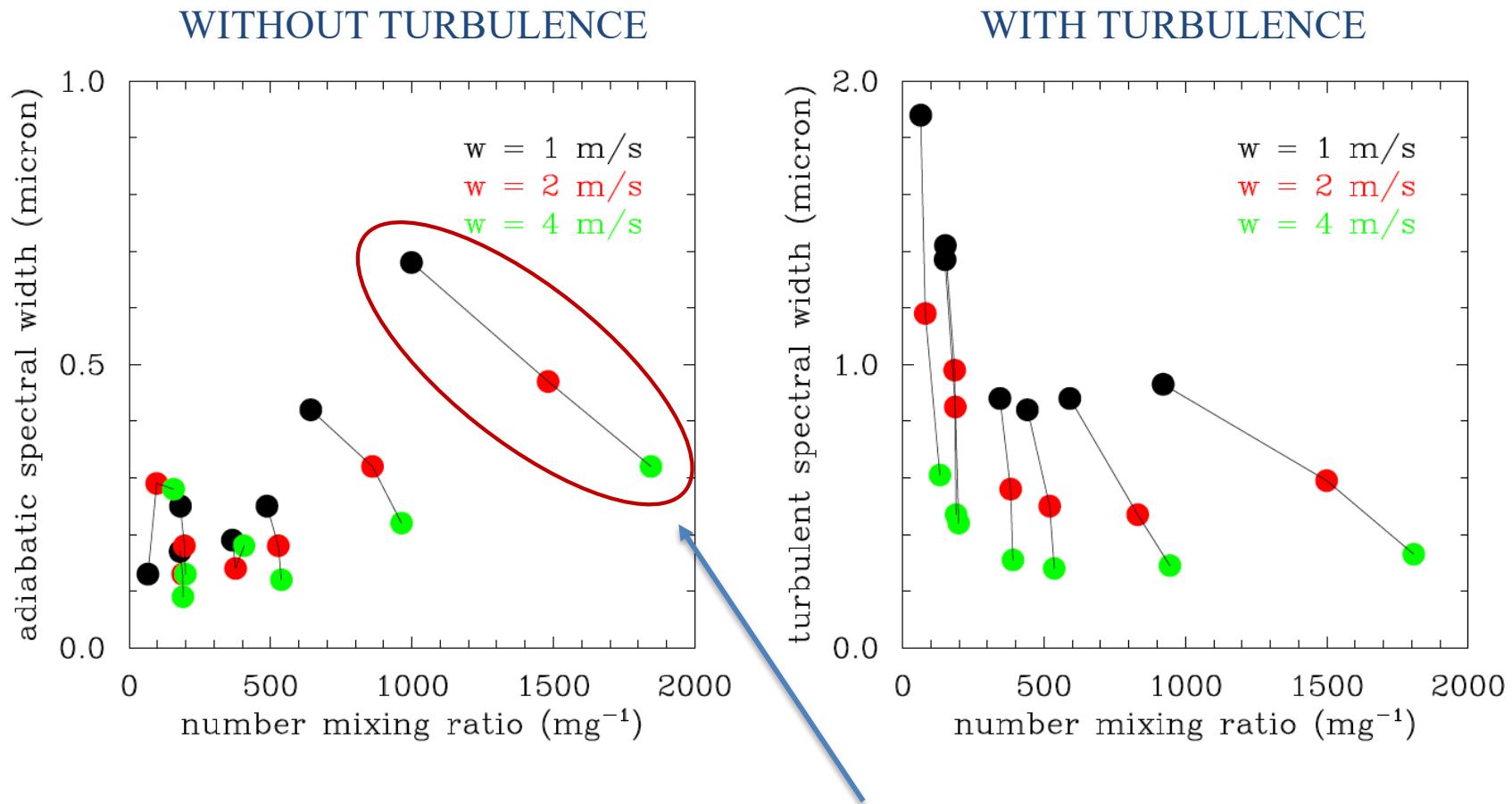
## Results for all dry CCN distributions

simulation	w (m/s)	NO TURB	Number m.r. (1/mg)	Width (micron)	WITH TURB	Number m.r. (1/mg)	Width (micron)	Turb. width enhmt.
POL	1		487	0.25		441	0.84	3.4
	2		527	0.18		520	0.50	2.8
	4		538	0.12		526	0.28	2.3
PRI	1		66	0.13		64	1.88	14.5
	2		97	0.29		80	1.18	4.1
	4		157	0.28		132	0.61	2.2
REV-POL	1		180	0.17		151	1.42	8.4
	2		189	0.13		184	0.98	7.5
	4		190	0.09		189	0.47	5.2
REV-PRI	1		365	0.19		344	0.88	4.6
	2		376	0.14		382	0.56	4.0
	4		406	0.18		390	0.31	1.7
G-POL	1		998	0.68		921	0.93	1.4
	2		1481	0.47		1499	0.59	1.3
	4		1845	0.32		1807	0.33	1.0
G-1000	1		642	0.42		591	0.88	2.1
	2		860	0.32		831	0.47	1.5
	4		963	0.22		945	0.29	1.3
G-PRI	1		181	0.25		150	1.37	5.5
	2		195	0.18		186	0.85	4.7
	4		199	0.13		198	0.44	3.4

# Results for all dry CCN distributions

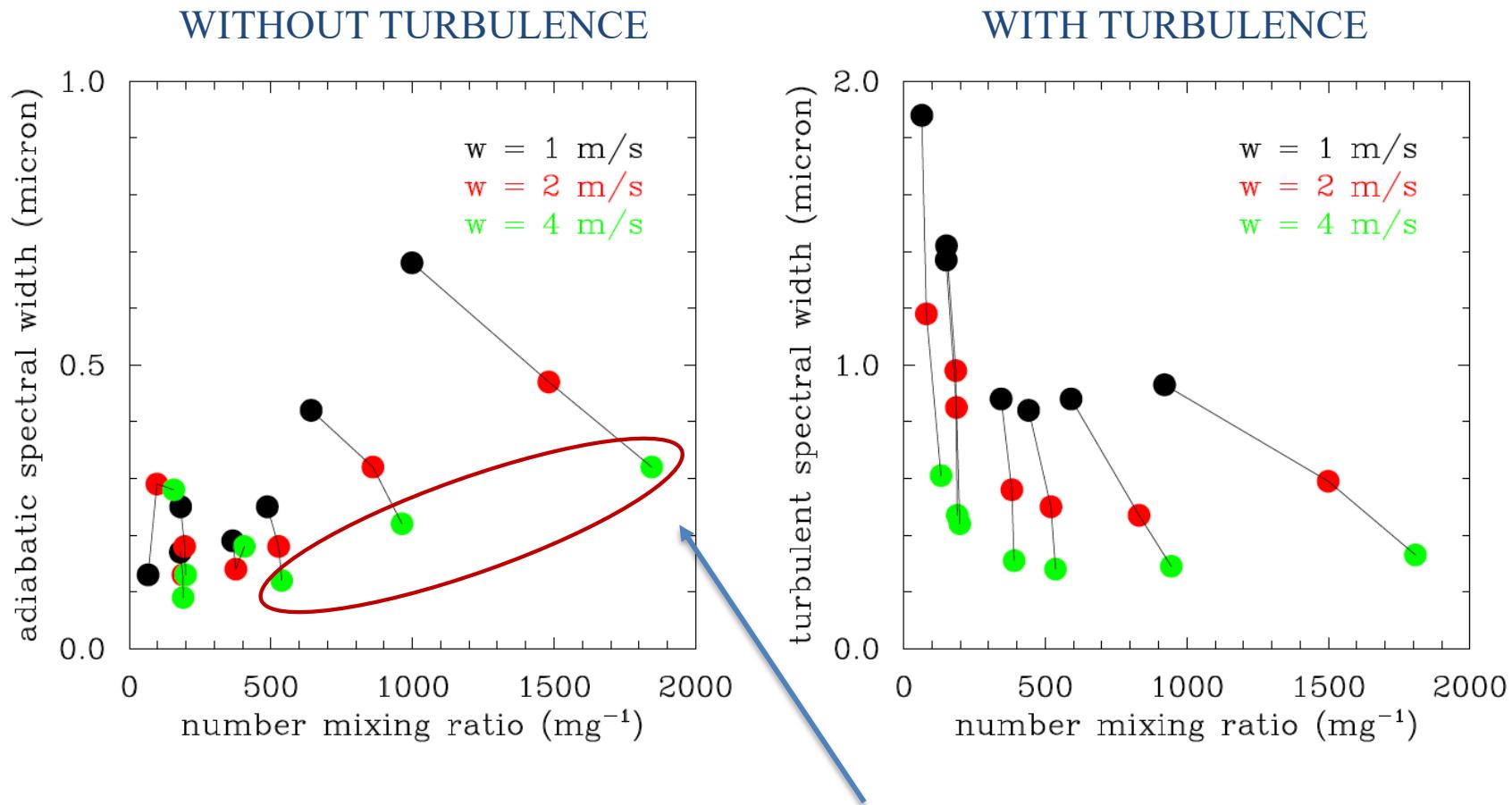


# Results for all dry CCN distributions



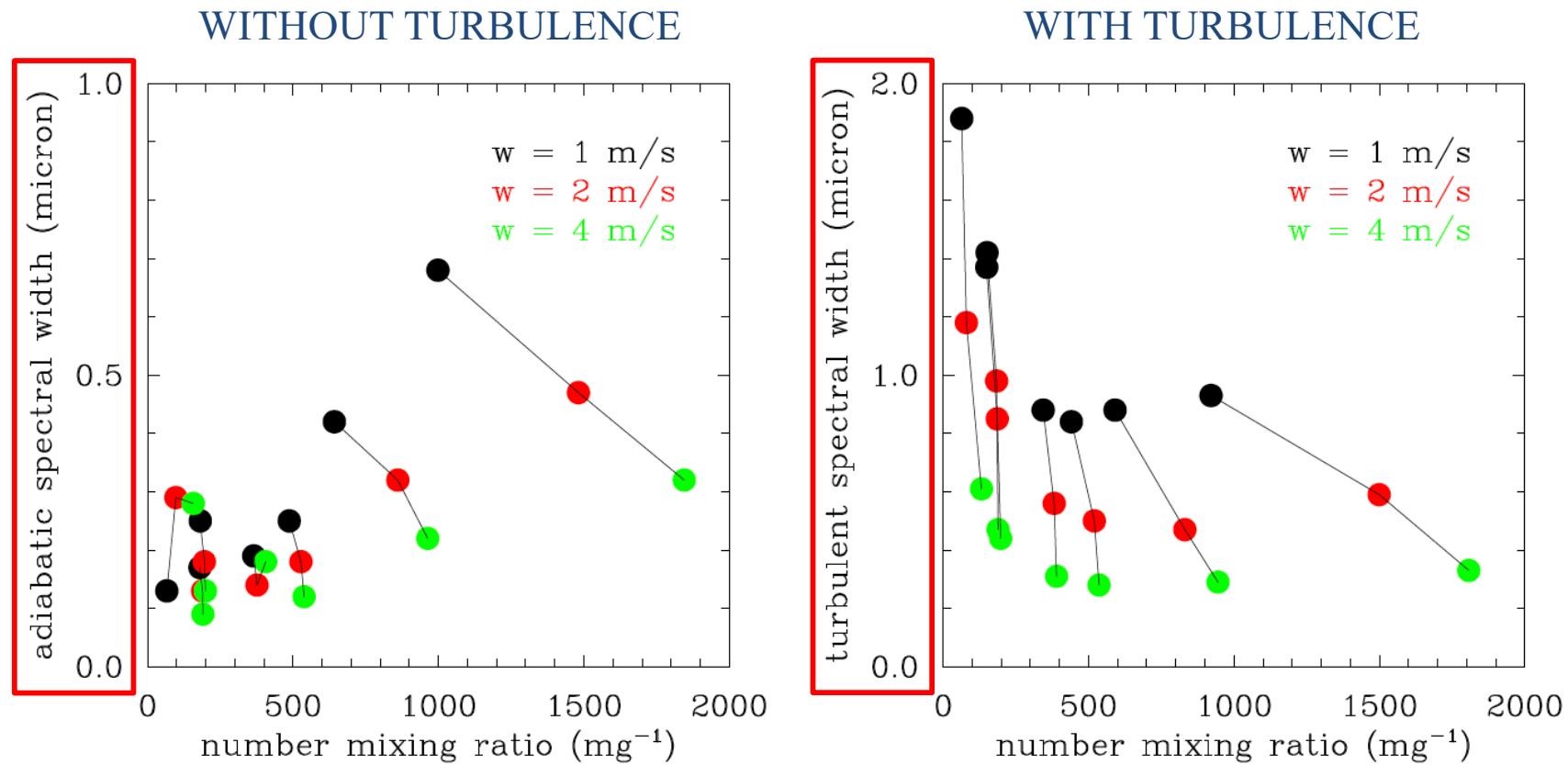
the same CCN, different updrafts

# Results for all dry CCN distributions

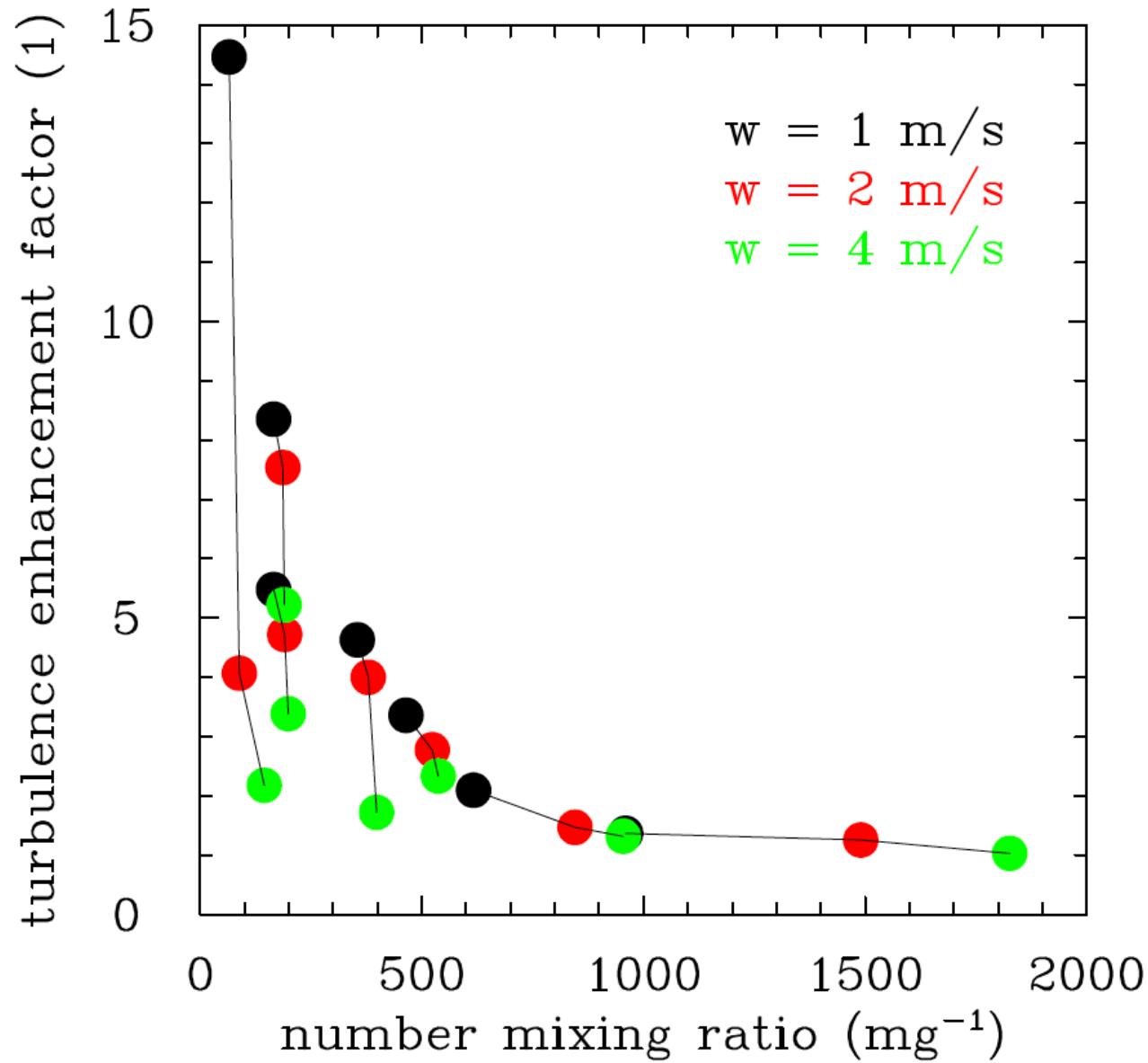


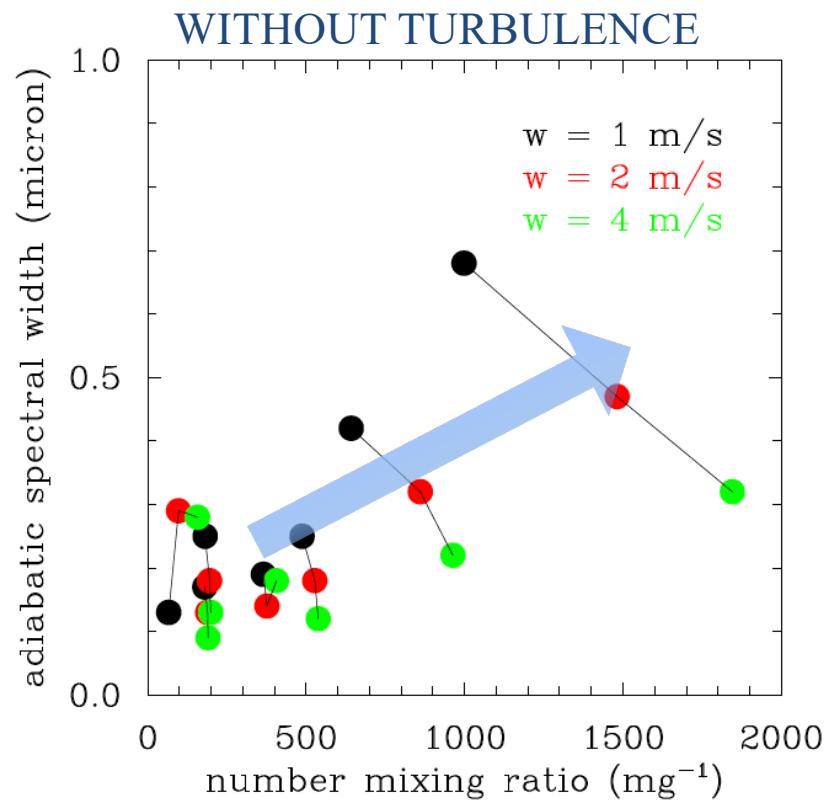
different CCN, the same updrafts

# Results for all dry CCN distributions

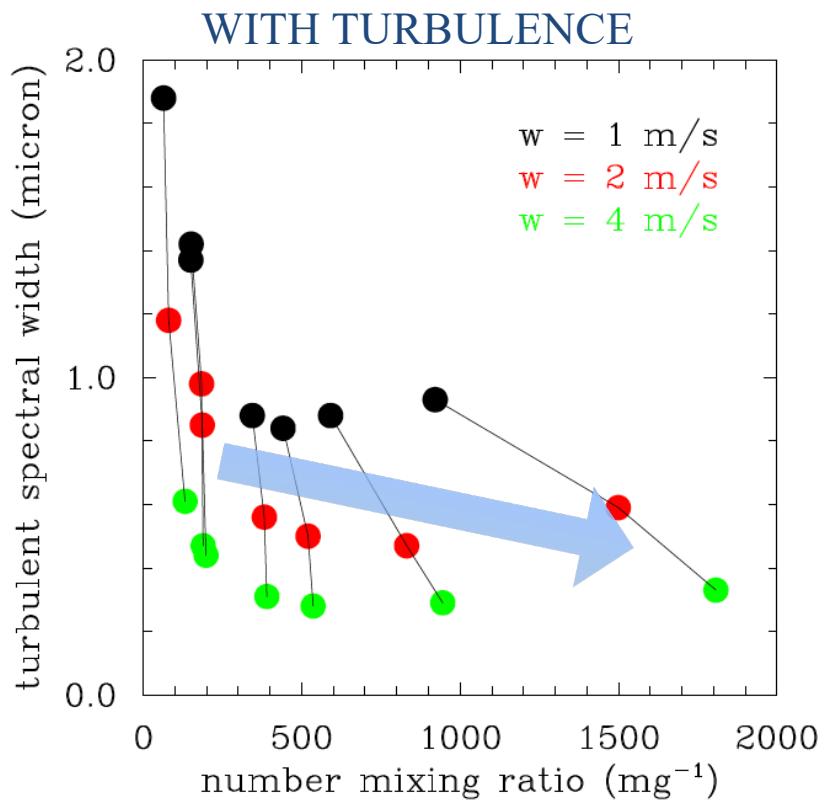


## Results for all dry CCN distributions





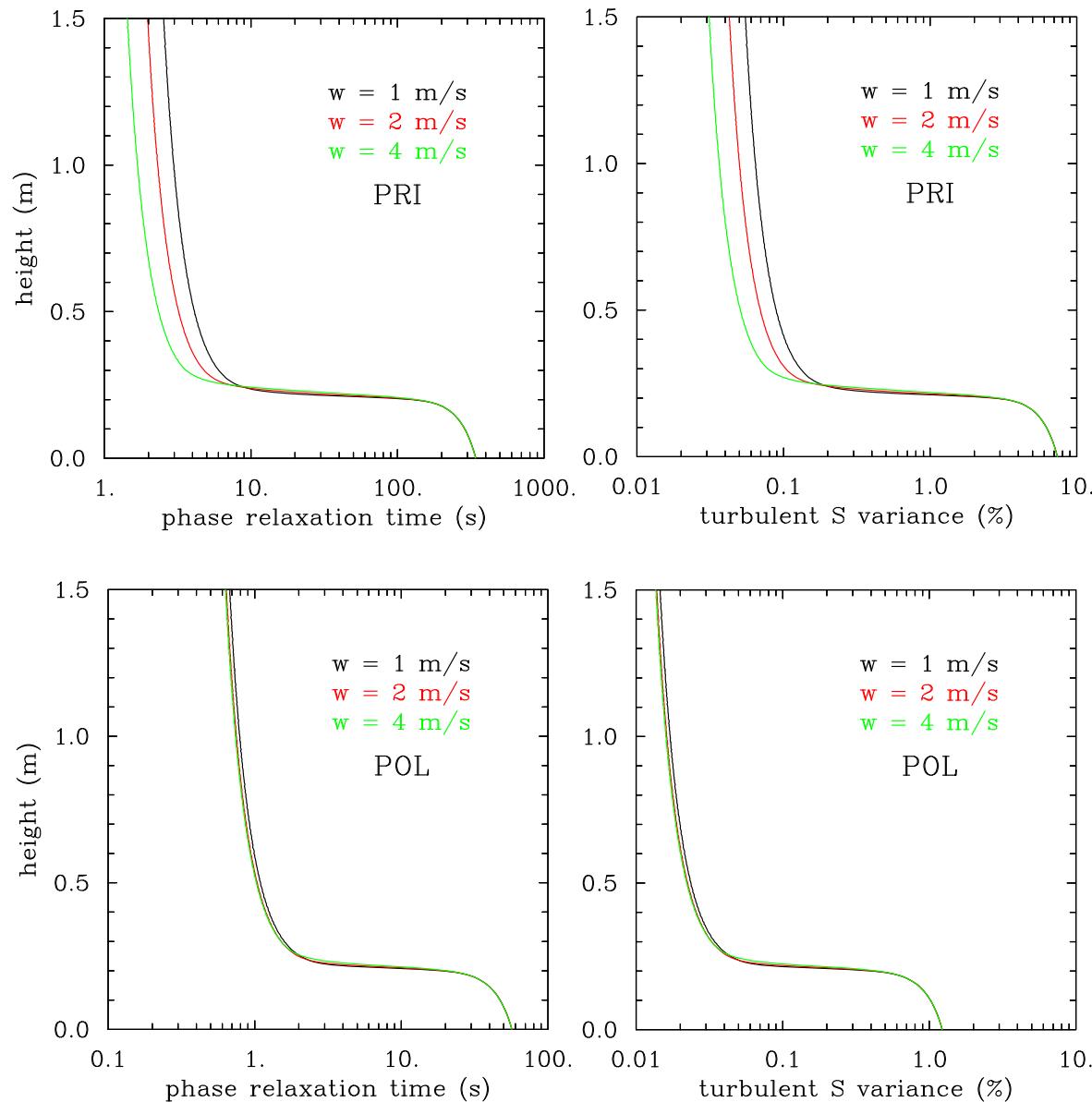
Spectral width tends to  
**increase** with droplet  
 concentration



Spectral width tends to  
**decrease** with droplet  
 concentration

# Where the reversal comes from?

## Pristine clouds feature longer phase relaxation time and thus larger supersaturation fluctuations!



$$\frac{dS'_i}{dt} = a_1 w'_i - \frac{S'_i}{\tau}$$

For the quasi-equilibrium supersaturation:

$$S_{qe} = a_1 \tau w$$

$$\sigma_S = a_1 \tau \sigma_w$$

$\sigma_w = 0.54 \text{ m sec}^{-1}$  is the vertical velocity variance

How to understand larger spectral widths in observations when compared to adiabatic parcel simulations?

How to understand opposite trends in observations and adiabatic parcel simulations?

The answer to both questions:

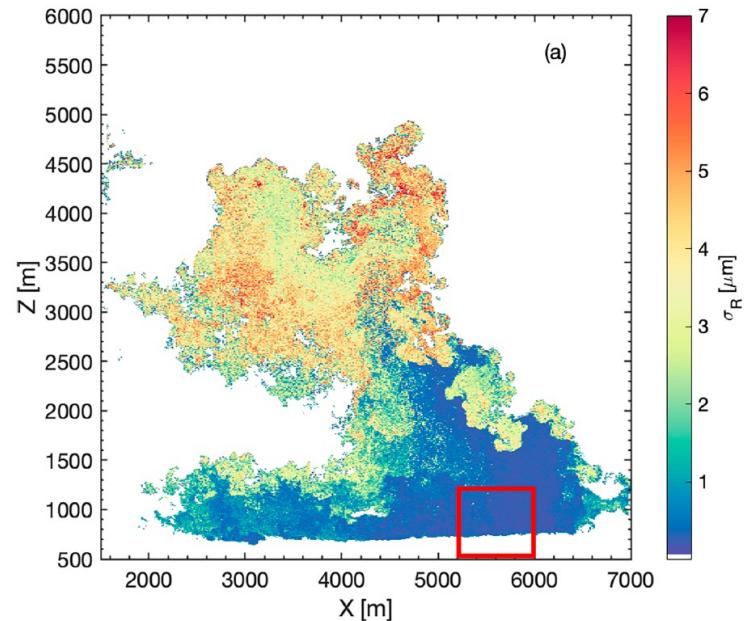
*Cloud turbulence impact on formation and growth of cloud droplets!*

Is there a support for this claim in 3D cloud simulations?

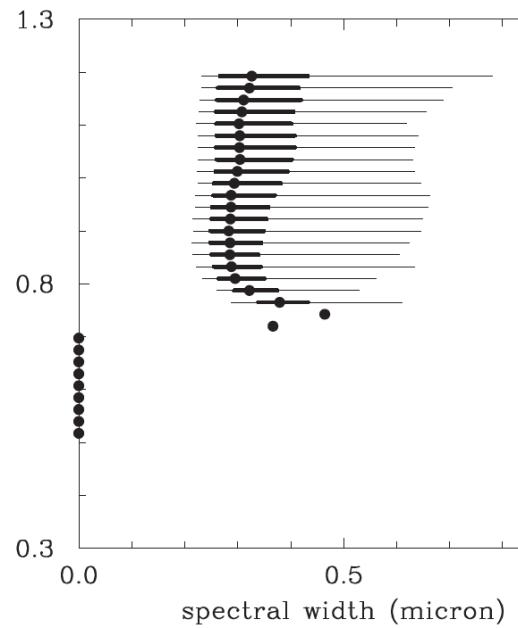
## Untangling the Broadening of Adiabatic Cloud Droplet Spectra through Eddy Hopping in a High-Resolution Cumulus Congestus Simulation

WOJCIECH W. GRABOWSKI,<sup>a</sup> KAMAL KANT CHANDRAKAR,<sup>a</sup> AND HUGH MORRISON<sup>a</sup>

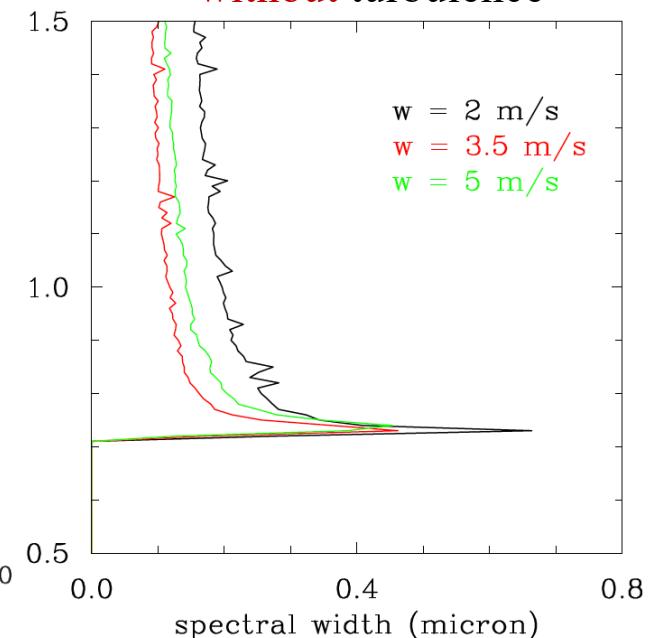
<sup>a</sup> MMM Laboratory, NSF National Center for Atmospheric Research, Boulder, Colorado



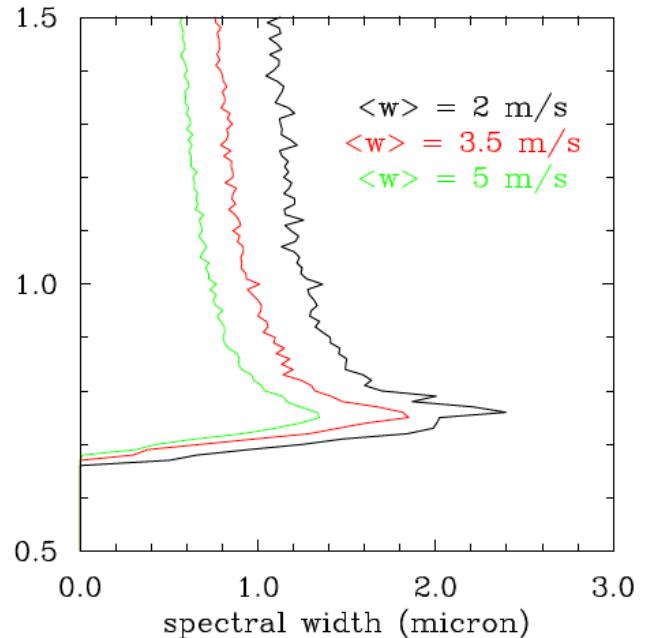
3D cloud model

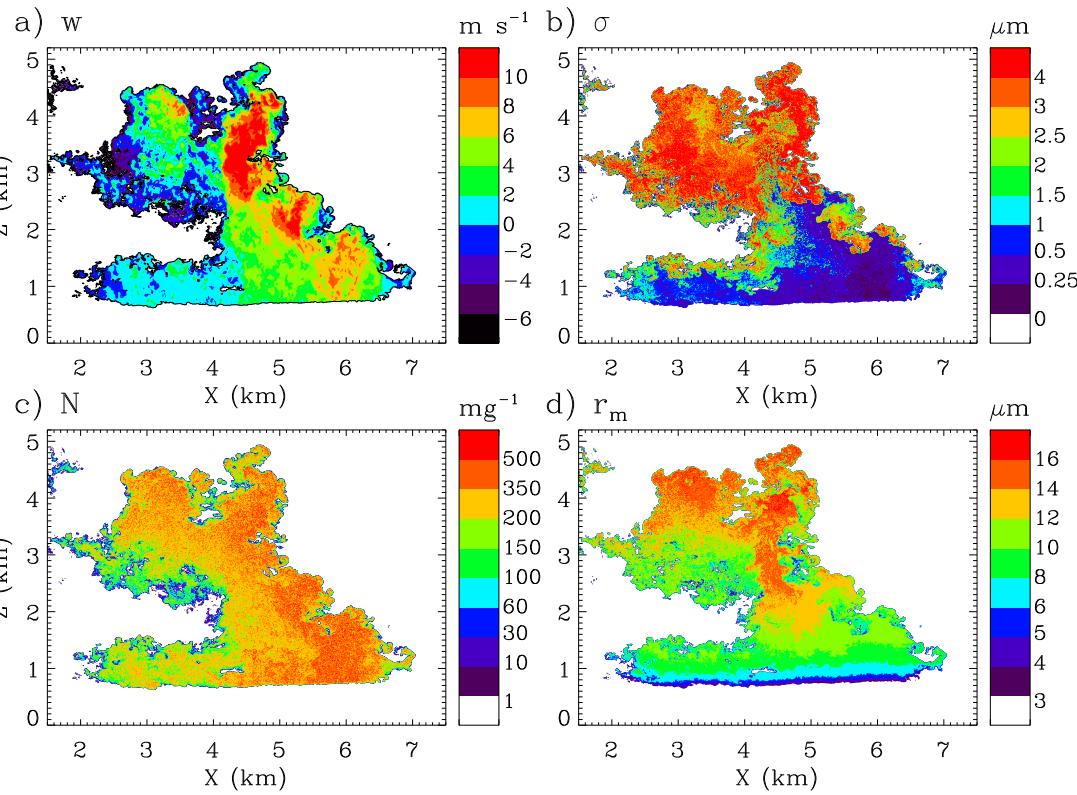


1D updraft model  
without turbulence



1D updraft model  
with turbulence





AUGUST 2025

GRABOWSKI ET AL.

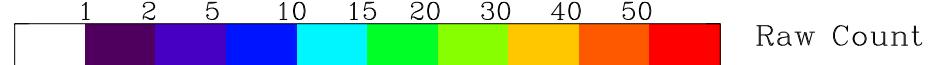
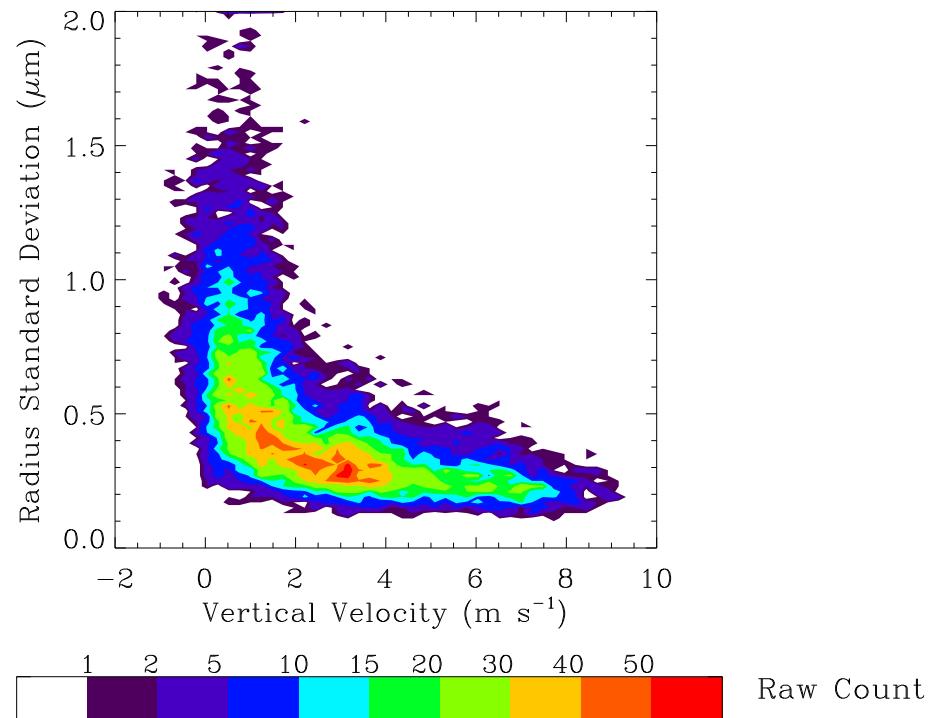
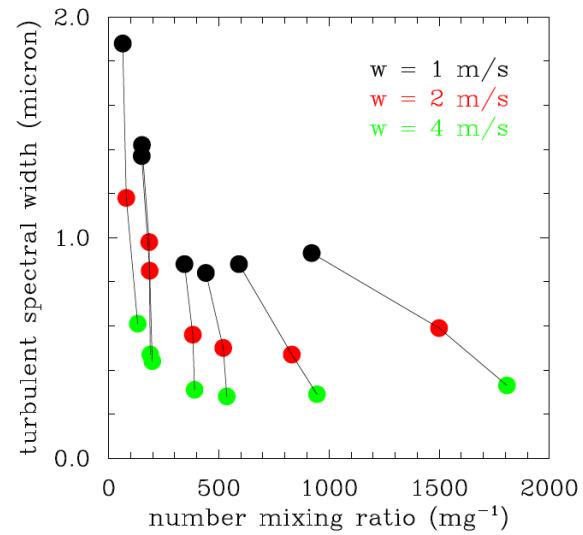
1585

Untangling the Broadening of Adiabatic Cloud Droplet Spectra through Eddy Hopping in a High-Resolution Cumulus Congestus Simulation

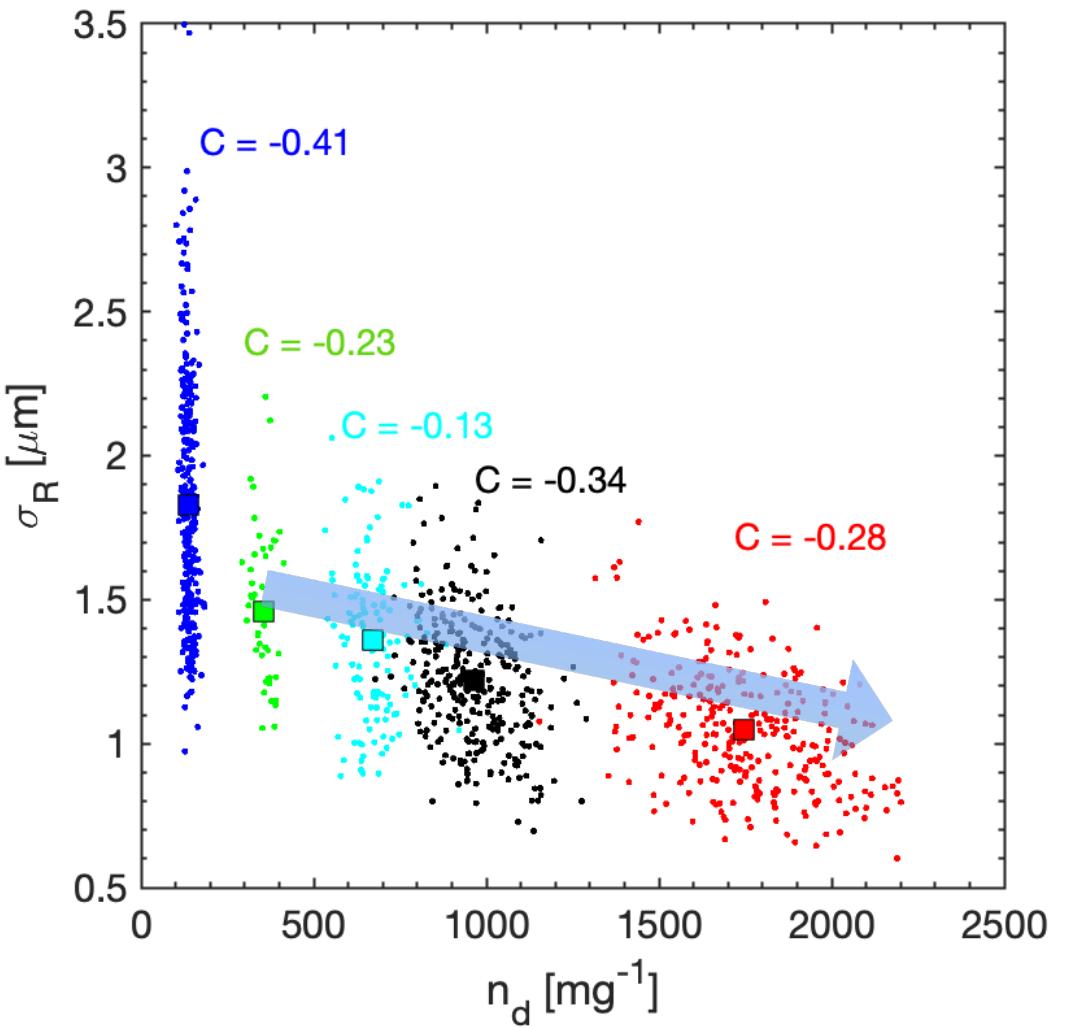
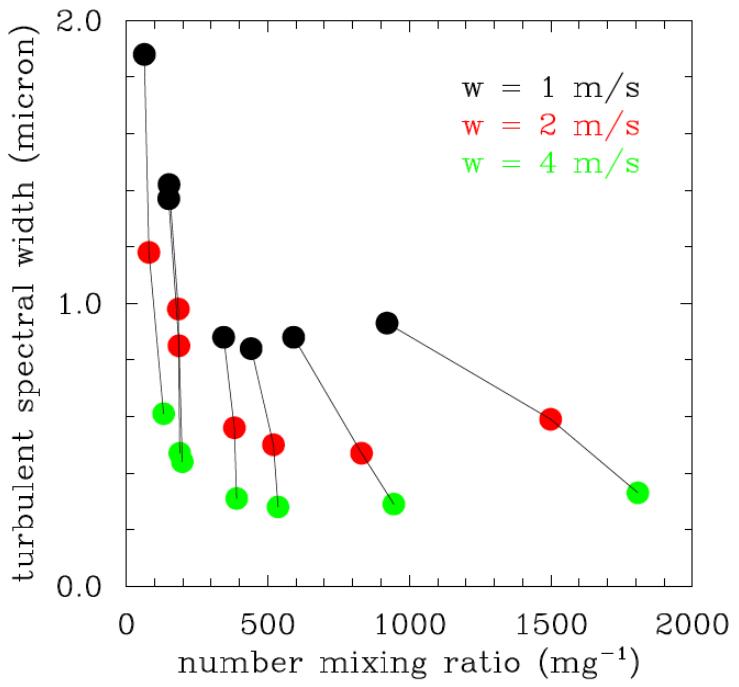
WOJCIECH W. GRABOWSKI,<sup>a</sup> KAMAL KANT CHANDRAKAR,<sup>a</sup> AND HUGH MORRISON<sup>a</sup>

<sup>a</sup> MMM Laboratory, NSF National Center for Atmospheric Research, Boulder, Colorado

The same 3D high-res 3D simulation



Similar 3D lower-resolution  
cloud simulations with different  
dry CCN spectra: pristine to  
polluted conditions



## Summary:

In agreement with previous studies, adiabatic spectra *without turbulence* are typically narrow. Polluted CCN result in wider adiabatic droplet spectra.

*With turbulence*, droplet spectra simulated by the idealized 1D adiabatic Eulerian – Lagrangian vertical air current are wider, especially in pristine conditions. This agrees with observations of natural clouds and with observations and numerical simulations of turbulent laboratory clouds.

Larger turbulence impact in pristine conditions is explained by a longer phase relaxation time that implies larger turbulent supersaturation fluctuations for the same turbulent vertical velocity fluctuations.

